



Evaporation-driven transport and precipitation of salt in porous media: A multi-domain approach

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EGU General Assembly - 2014

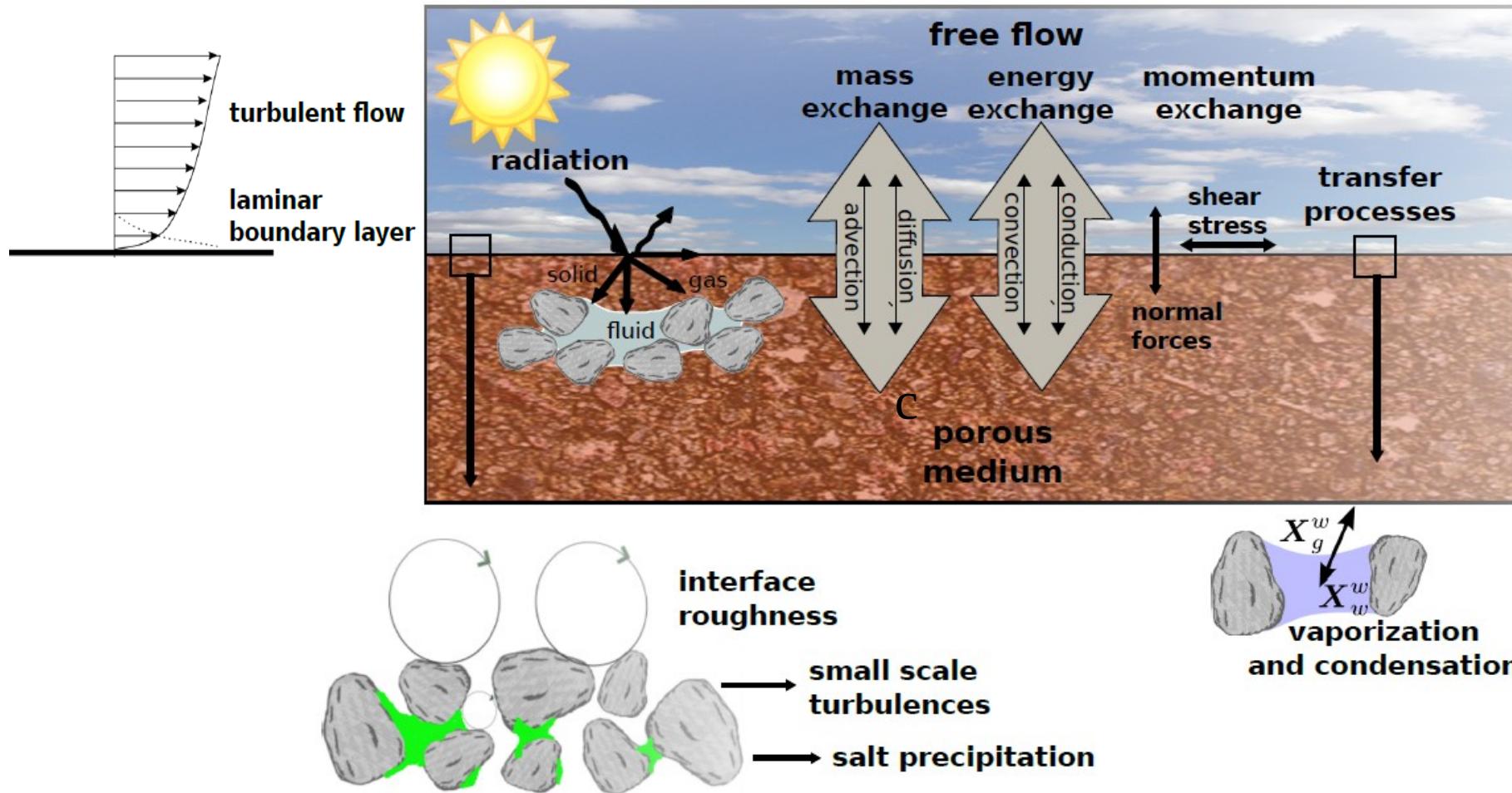


Overview

- Motivation
- Model Concept
- Results
- Outlook

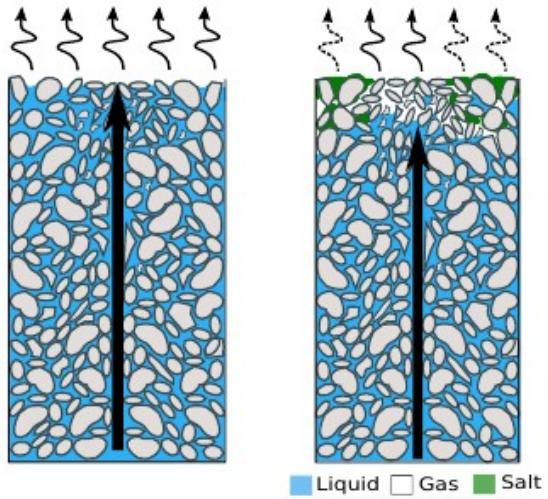


Motivation



"A coupling concept for two-phase compositional porous-medium and single-phase compositional free flow", *Mosthaf et al., 2011*

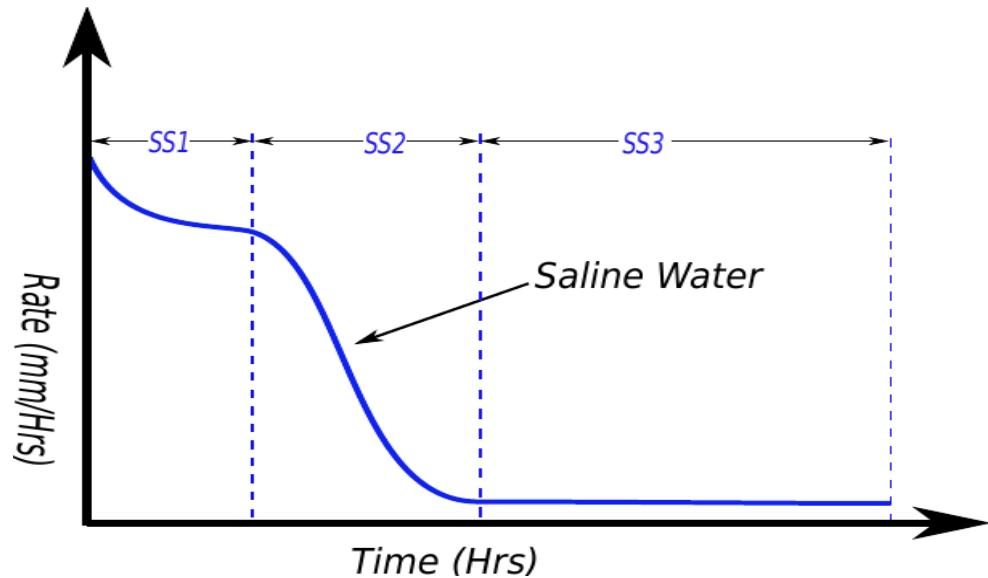
Stages of saline water evaporation



(a) SS1

(b) SS2

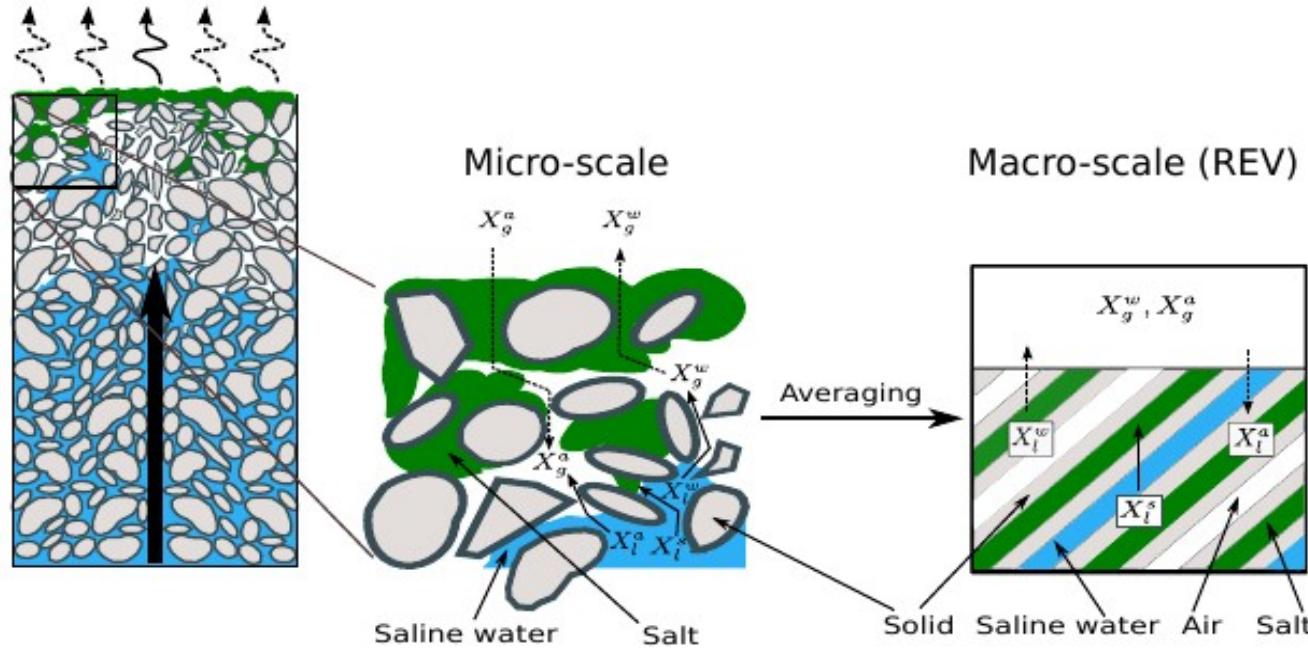
(c) SS3



- Stages of evaporation:
 - SS1: High evaporation rate
 - SS2: Evaporation rate falls subsequently
 - SS3: Constant low evaporation rate

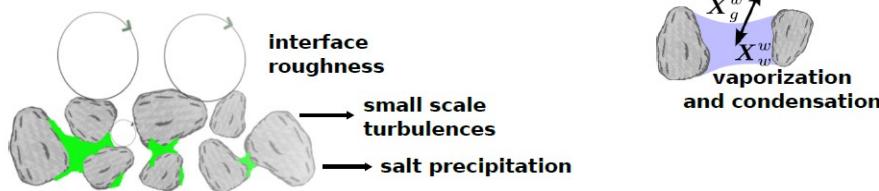
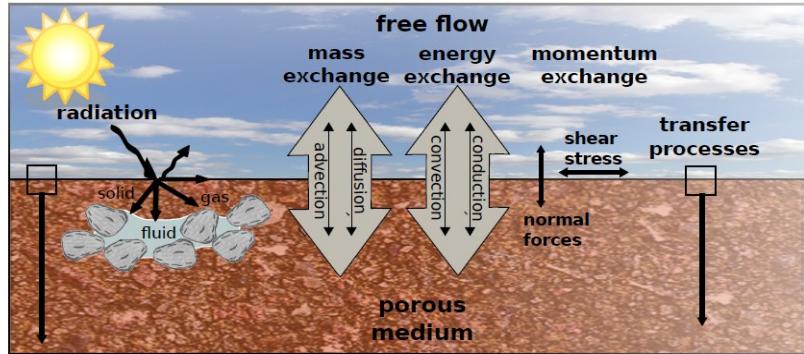
Salinization: Interplay between salt transport, evaporation dynamics and salt precipitation

Macro-scale (REV)

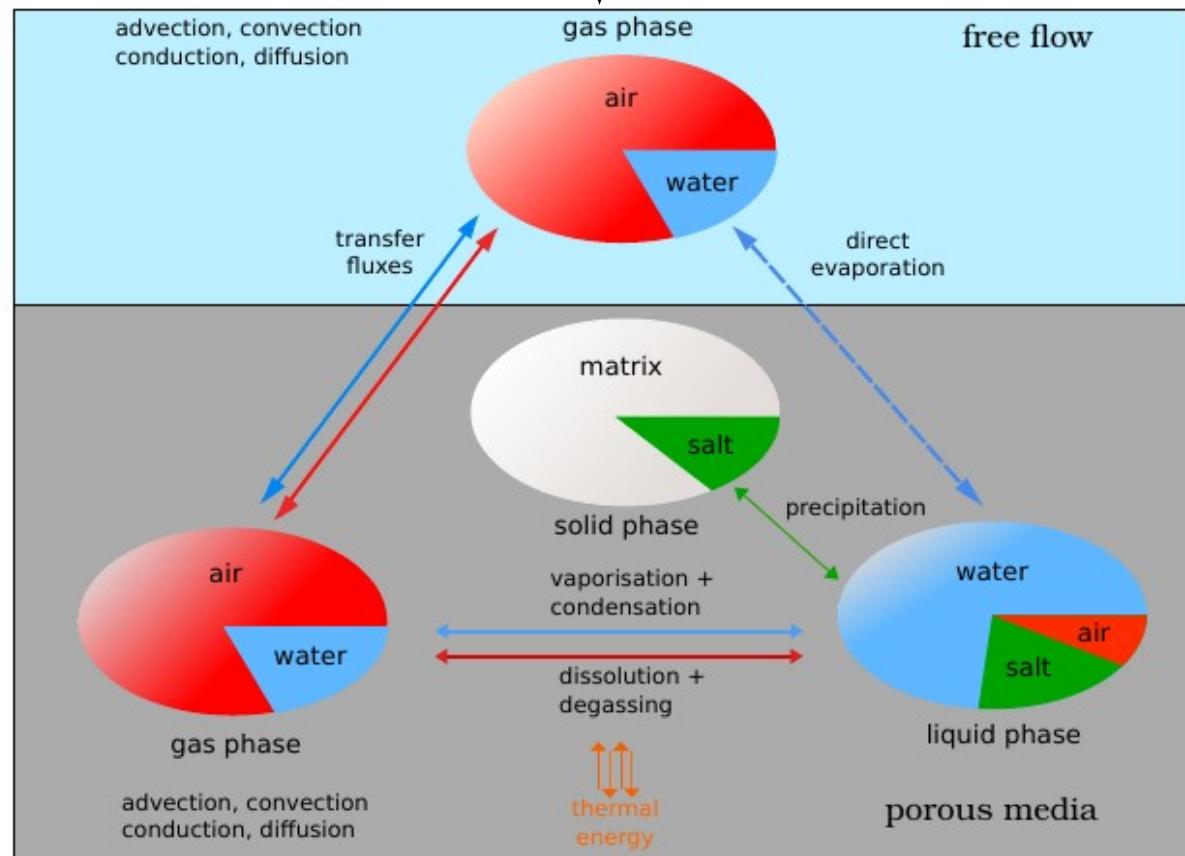


Micro-scale to macro-scale transition

Model Concept



“A mathematical/numerical model requires an idealization of the physical processes in a natural system in such a way that their characteristic properties are maintained .”



Porous-media Equations : (p_g , s_w , x_l^{NaCl})

- Multi-phase-multi-component Darcy flow
- Mass conservation for each component :

$$\sum_{\alpha} \underbrace{\frac{\partial(\phi \varrho_{mol,\alpha} S_{\alpha} x_{\alpha}^{\kappa})}{\partial t}}_{\text{storage}} - \sum_{\alpha} \underbrace{\nabla \cdot \left[\frac{k_{r\alpha}}{\mu_{\alpha}} \varrho_{mol,\alpha} x_{\alpha}^{\kappa} \mathbf{K} (p_{\alpha} - \varrho_{\alpha} g) \right]}_{\text{advection}} - \sum_{\alpha} \underbrace{\nabla \cdot [D_{pm,\alpha}^{\kappa} \varrho_{mol,\alpha} \nabla x_{\alpha}^{\kappa}]}_{\text{diffusion}} = \sum_{\alpha} \underbrace{q_{\alpha}^{\kappa}}_{\text{source/sink}}$$

- Salt precipitation:

$$q_{\alpha}^{\kappa} = \begin{cases} \frac{\partial(\phi \varrho_{mol,l} S_l (x_l^{\text{NaCl}} - x_{l,max}^{\text{NaCl}}))}{\partial t} & \text{for } \kappa = \text{NaCl, } \alpha = l \\ 0 & \text{else} \end{cases}$$

$$\frac{\partial(\phi_s^{\text{NaCl}} \varrho_{mol,s}^{\text{NaCl}})}{\partial t} + q_l^{\text{NaCl}} = 0$$

“Analytical solution to evaluate salt precipitation during CO₂ injection in saline aquifers”, Zeidouni *et al.*, 2009

Porous-media Equations

- Local thermodynamic equilibrium:

- Local thermal equilibrium:

$$T_l = T_g = T_s = T$$

- Chemical equilibrium accounts for the mass transfer across different phases:

$$p_g = \sum_{\kappa} p_g^{\kappa} \quad p_g^{\kappa} = x_g^{\kappa} p_{\text{sat}}^{\kappa} \quad p_g^{\kappa} = x_w^{\kappa} H_w^{\kappa}$$

- Mechanical equilibrium is valid locally. Discontinuities in pressure exists across fluid-fluid-solid interface:

$$p_c = p_g - p_l$$

Porous-media Equations:(T)

- One energy balance equation:

$$\sum_{\alpha} \underbrace{\frac{\partial(\phi \varrho_{\alpha} u_{\alpha} S_{\alpha})}{\partial t}}_{\text{storage I}} + \sum_{\alpha} \underbrace{\frac{\partial(\phi_s^{\text{NaCl}} \varrho_s^{\text{NaCl}} c_s^{\text{NaCl}} T)}{\partial t}}_{\text{storage II}} + \sum_{\alpha} (1 - \phi_0) \underbrace{\frac{\partial(\varrho_s c_s T)}{\partial t}}_{\text{storage III}} \\ + \sum_{\alpha} \underbrace{\nabla \cdot (\varrho_{\alpha} h_{\alpha} \mathbf{v}_{\alpha})}_{\text{convection}} - \underbrace{\nabla \cdot (\lambda_{pm} T)}_{\text{conduction}} = 0$$

Where heat conductivity :

$$\lambda_{pm} = \lambda_{\text{eff},g} + \sqrt{S_l} (\lambda_{\text{eff},l} - \lambda_{\text{eff},g})$$

Effective heat conductivity :

$$\frac{\lambda_{\text{eff},\alpha}}{\lambda_{\alpha}} = \left(\frac{\lambda_s}{\lambda_{\alpha}} \right)^{0.28 - 0.757 \log \phi - 0.057 \log(\lambda_s / \lambda_{\alpha})}$$

“High Temperature Behaviour of rocks Associated with Geothermal Type Reservoirs”, Somerton et al., 1974

Porous-media Equations

Supplementary constraints:

- Total void-space within the porous matrix is occupied by liquid and gas phases:

$$S_g = 1 - S_l$$

- The secondary phase pressure is determined using capillary-pressure:

$$p_c(S_l) = p_g - p_l$$

- The mass and mole fractions of all components in each phase sums up to one:

$$X_l^w + X_l^a + X_l^{\text{NaCl}} = x_l^w + x_l^a + x_l^{\text{NaCl}} = 1$$

Fluid Properties:

$$\mu_l = 0.1 + 0.333X_l^{\text{NaCl}} + (1.65 + 91.9X_l^{\text{NaCl}})^3 + \exp\{-[0.42(X_l^{\text{NaCl}})^{0.8} - 0.17]^2 + 0.045\}T^{0.8}$$

$$\begin{aligned} \varrho_l = \varrho_w + 1000X_l^{\text{NaCl}} &\{0.668 + 0.44X_l^{\text{NaCl}} + [300p - 2400pX_l^{\text{NaCl}} \\ &+ T(80 + 3T - 3300X_l^{\text{NaCl}} - 13p + 47pX_l^{\text{NaCl}})] \times 10^{-6}\} \end{aligned}$$



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Free-flow Equations: (v_x , v_y , P_g , T , x_g^w)

- Stokes equation: (no turbulence - 1Phase)

$$\underbrace{\frac{\partial(\varrho_g \mathbf{v}_g)}{\partial t}}_{\text{storage}} + \underbrace{\nabla \cdot [p_g \mathbf{I} - \mu_g (\nabla \mathbf{v}_g + \nabla \mathbf{v}_g^T)]}_{\text{flux}} = \underbrace{\varrho_g \mathbf{g}}_{\text{body force}}$$

- Phase conservation:

$$\underbrace{\frac{\partial \varrho_g}{\partial t}}_{\text{storage}} + \underbrace{\nabla \cdot (\varrho_g v_g)}_{\text{advection}} = \underbrace{q_g}_{\text{source/sink}}$$

- Component conservation

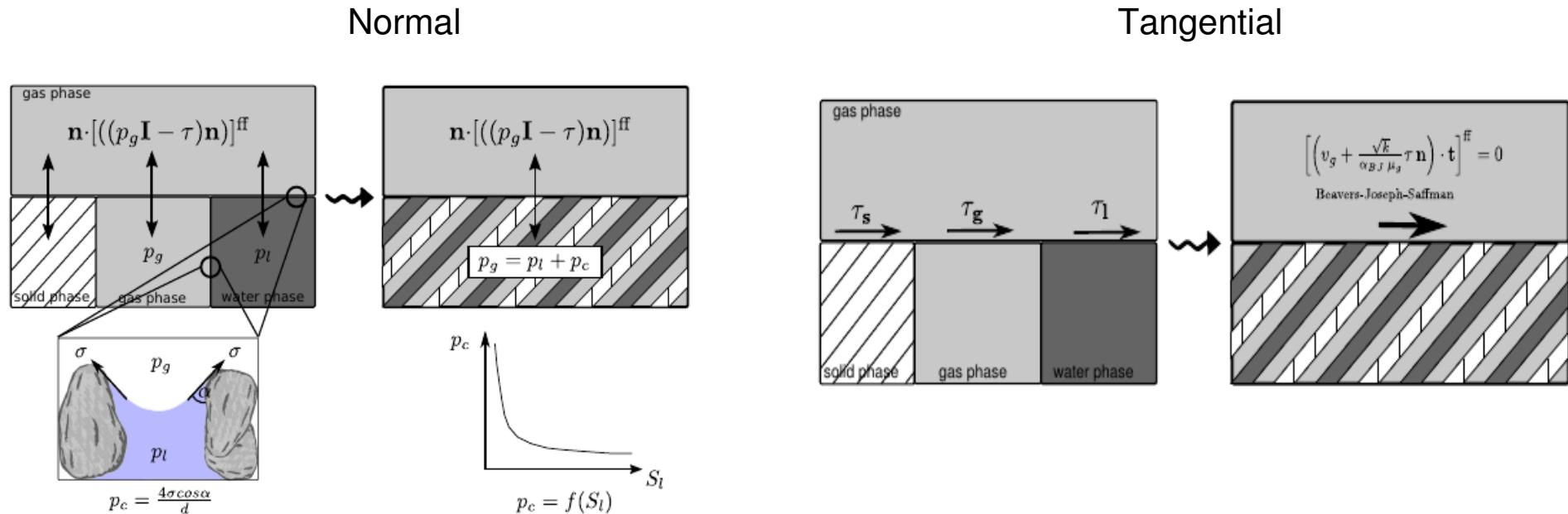
$$\underbrace{\frac{\partial(\varrho_{mol,g} x_g^\kappa)}{\partial t}}_{\text{storage}} + \underbrace{\nabla \cdot (\varrho_{mol,g} x_g^\kappa v_g)}_{\text{advection}} - \underbrace{\nabla \cdot (D_{pm,g}^\kappa \varrho_{mol,g} \nabla x_g^\kappa)}_{\text{diffusion}} = \underbrace{q_g^\kappa}_{\text{source/sink}}$$

- Energy balance equation:

$$\underbrace{\frac{\partial(\varrho_g u_g)}{\partial t}}_{\text{storage}} + \underbrace{\nabla \cdot (\varrho_g h_g \mathbf{v}_g)}_{\text{convection}} - \underbrace{\nabla \cdot (\lambda_g \nabla T)}_{\text{conduction}} = \underbrace{q_T}_{\text{source/sink}}$$

Coupling at the ff-pm interface

- Mechanical equilibrium:

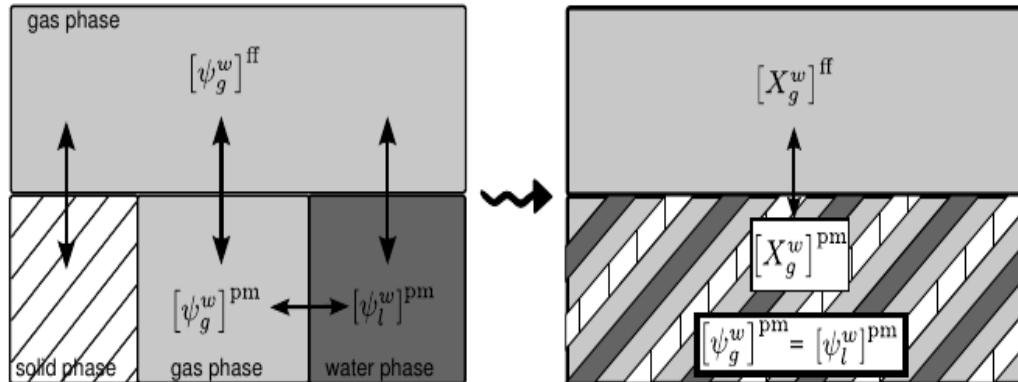


- Continuity of phase and component fluxes:

$$\underbrace{[\varrho_g \mathbf{v}_g \cdot \mathbf{n}]^{ff}}_{\text{Gas flux}} = - \underbrace{[(\varrho_g \mathbf{v}_g + \varrho_l \mathbf{v}_l) \cdot \mathbf{n}]^{pm}}_{\text{Total mass flux}}$$

Coupling at the ff-pm interface

- Chemical equilibrium:



- Continuity of chemical potential between phases inside the porous medium
- Continuity of mass or mole fraction at the interface

- Thermal equilibrium:

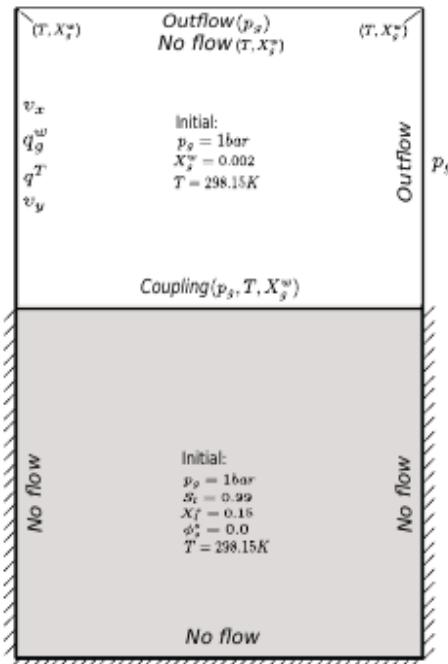
- local thermal equilibrium:

$$[T]^{ff} = [T]^{pm}$$

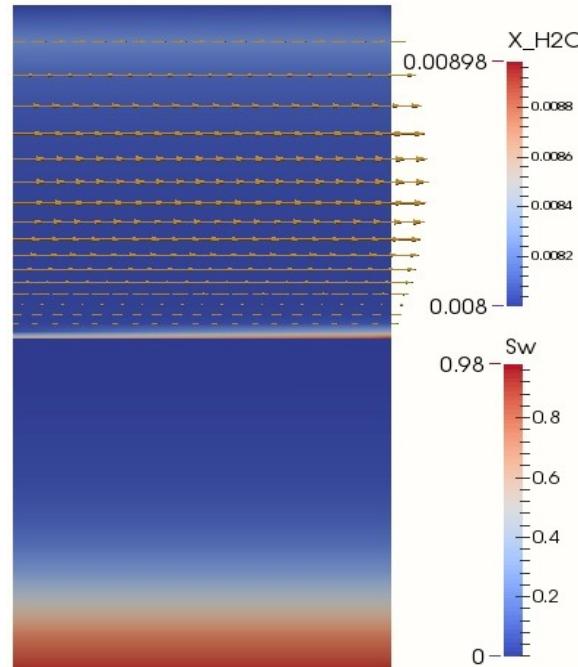
- Continuity of heat flux:

$$\underbrace{[(\varrho_g h_g \mathbf{v}_g - \lambda_g \nabla T) \cdot \mathbf{n}]^{ff}}_{\text{heat flux gas phase}} = -\underbrace{[(\varrho_g h_g \mathbf{v}_g + \varrho_l h_l \mathbf{v}_l - \lambda_{pm} \nabla T) \cdot \mathbf{n}]^{pm}}_{\text{Total heat flux}}$$

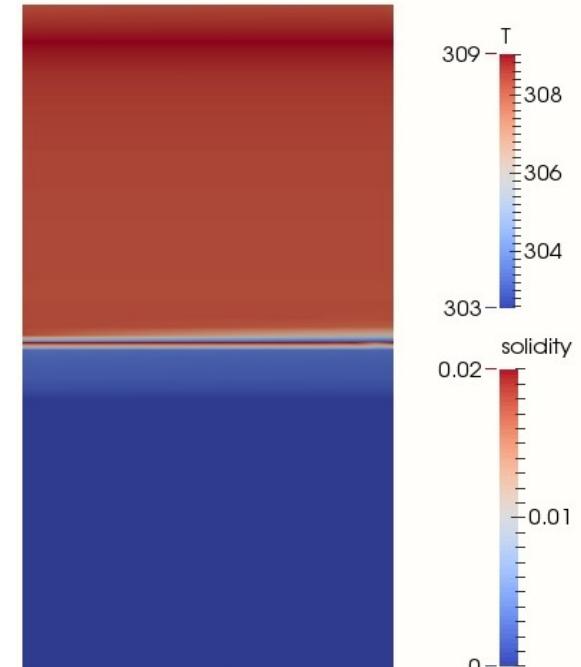
Mulit-domain: Coupled problem



Numerical example

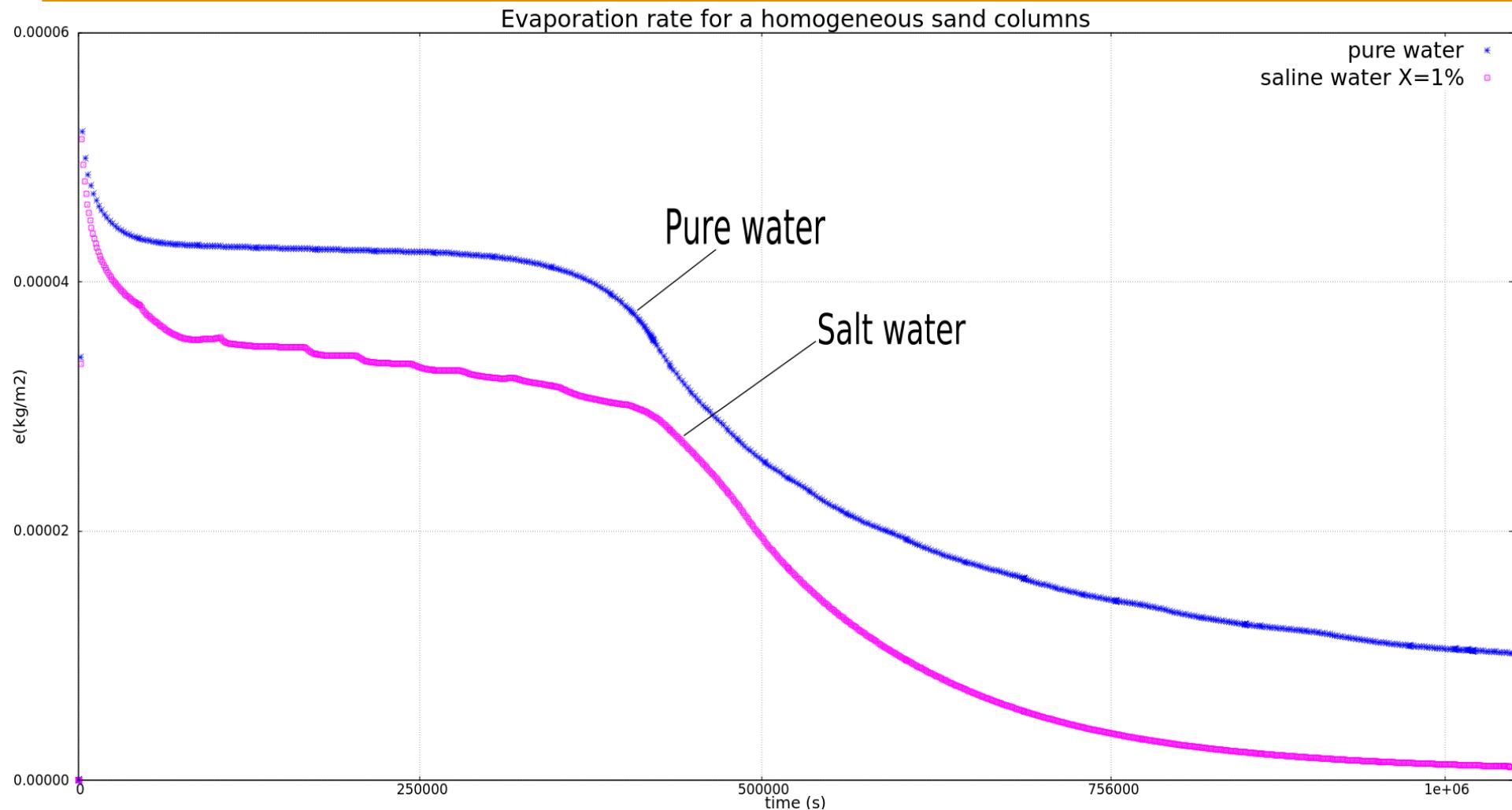


Drying



Salinization

Effect of salt: Case II



- Osmotic potential combined with pore clogging reduce vapour pressure



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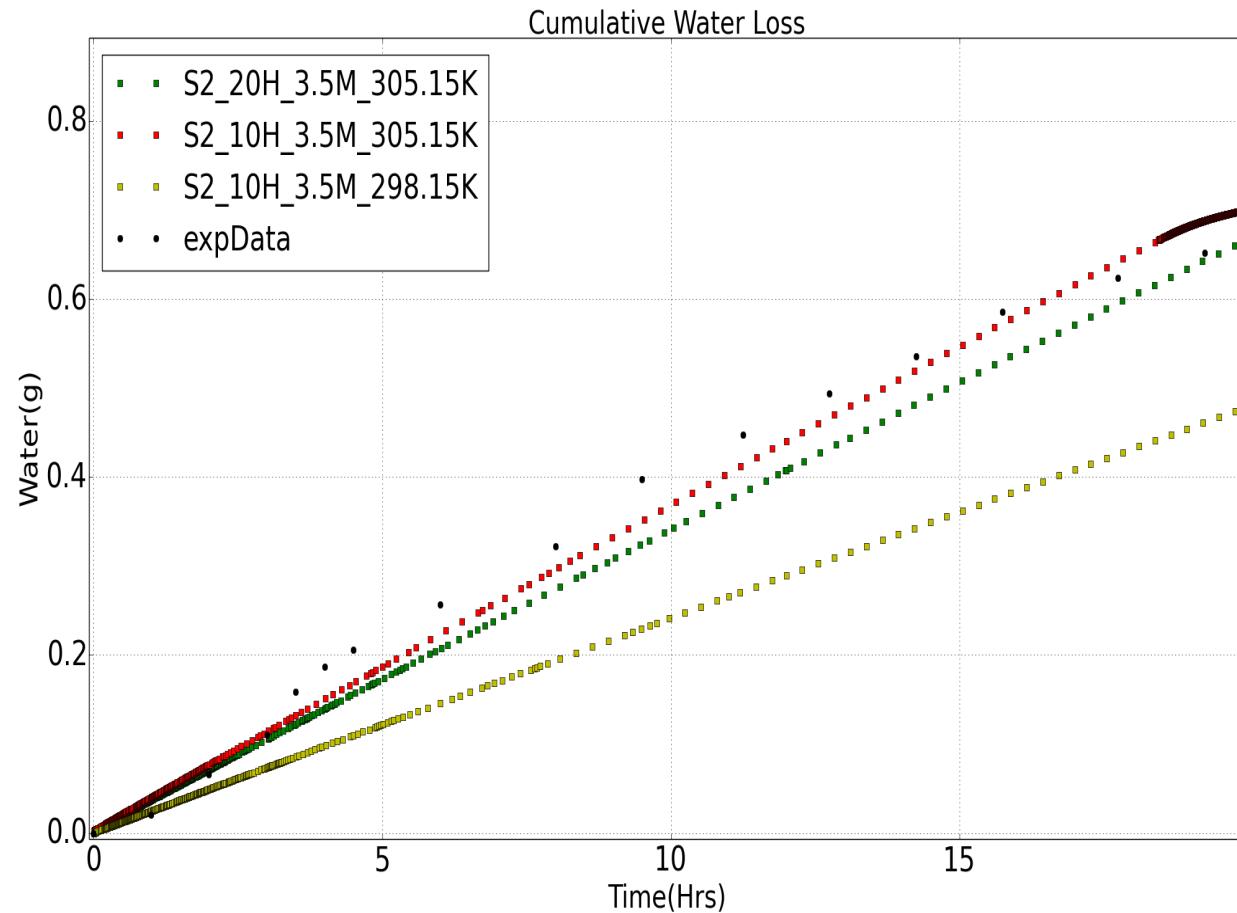


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Validation



$$K = 2.65e - 10 [m^2]$$

$$\phi = 0.37$$

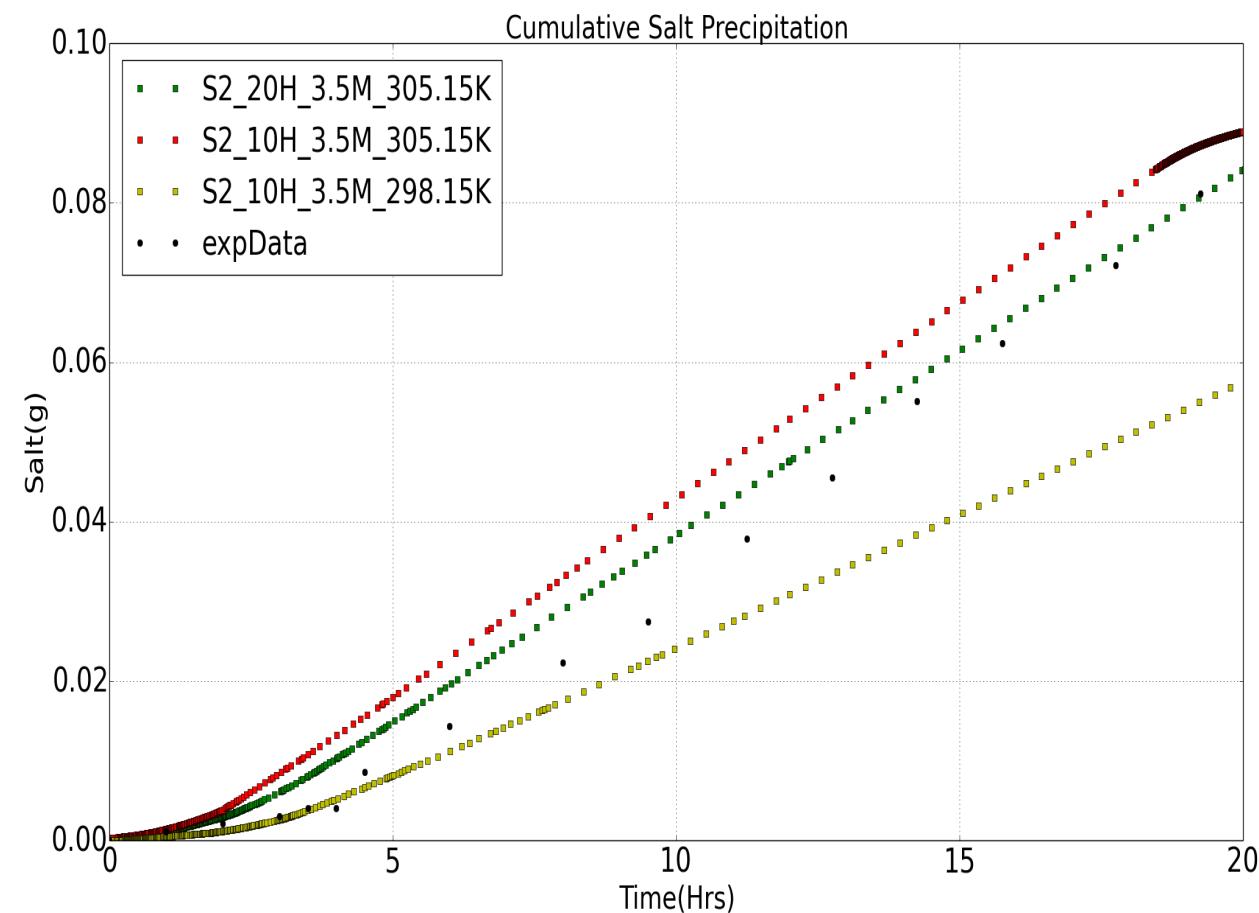
$$\alpha_{vg} = 6.02371e - 4$$

$$n_{vg} = 12.18$$

$$X_w^{NaCl} = 0.20454(3.5M)$$

“Pore-scale dynamics of salt precipitation in drying porous media”, Rad *et al.*, 2013

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Conclusion

- The model is capable to predict evaporation dynamics for non-saline, saline and hyper-saline scenarios.
- One can analyse the influence of variation in free-flow and porous-media parameters on evaporation dynamics and salinization.
- Validation cases clearly shows that the numerical simulations are in good agreement with the experimental data.

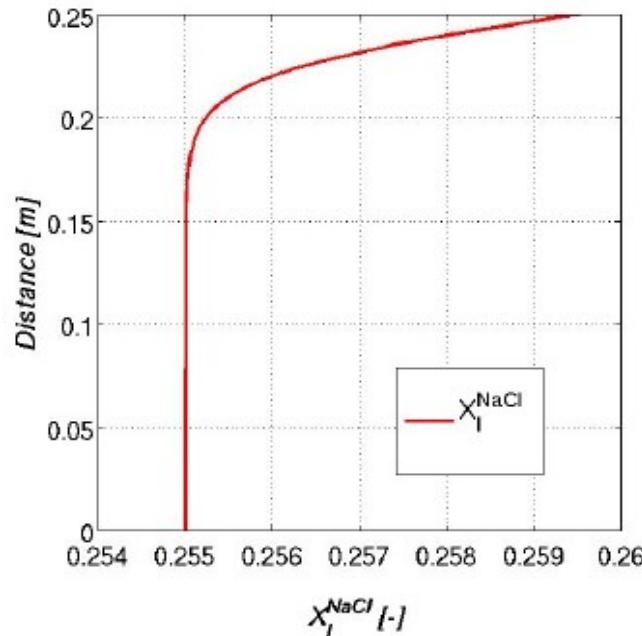
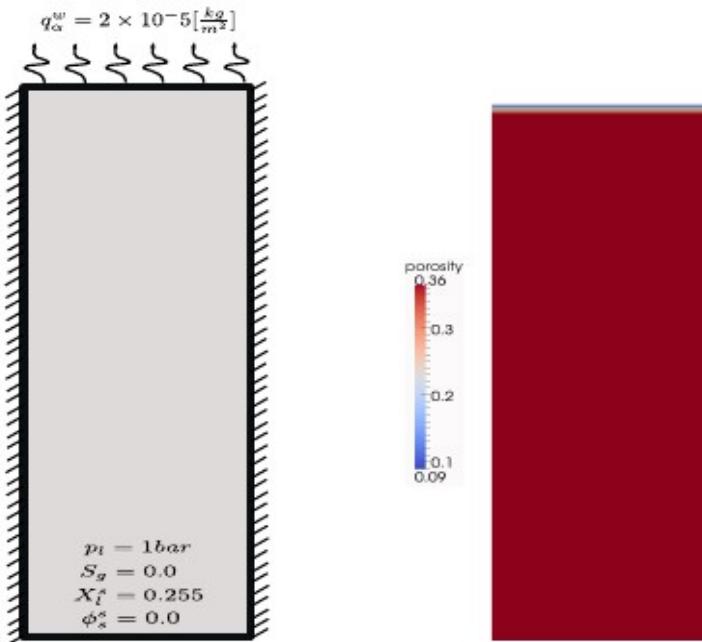
Outlook

Future Work:

- Reactive precipitation approach (under testing)
- Precipitation analysis for different salts (e.g. NaCl and NaI)
- Parameter analysis for free-flow and porous media
- Effect of random heterogeneities



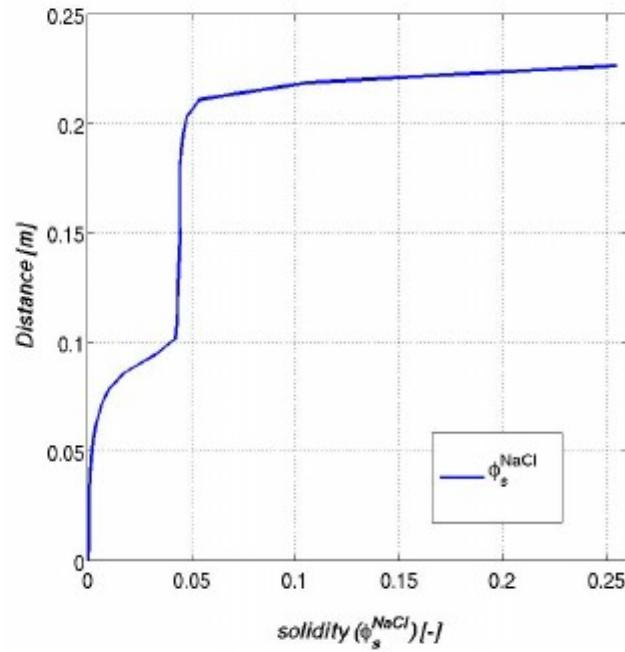
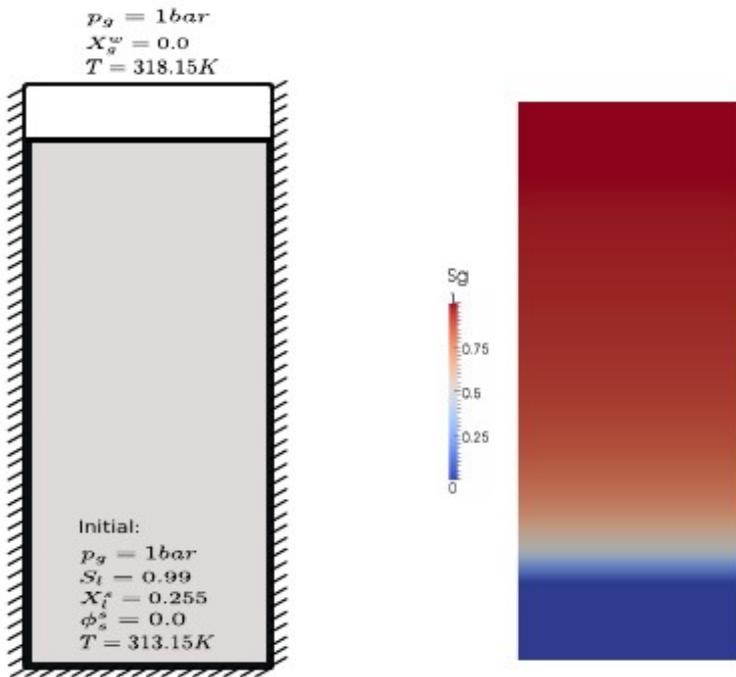
Single-domain PM problem: Case I



Dissolved NaCl distribution in a fully saturated homogeneous sand column

- Dirichlet BC at the bottom ensures the domain to be fully saturated.
- Fixed flux BC on top.

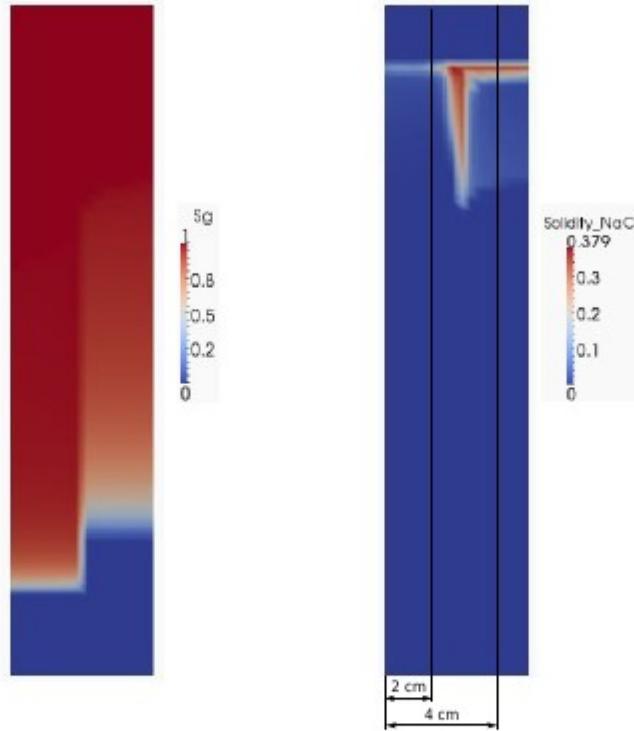
Single-domain PM problem: Case II



Evaporation driven NaCl precipitation in an unsaturated homogeneous sand column

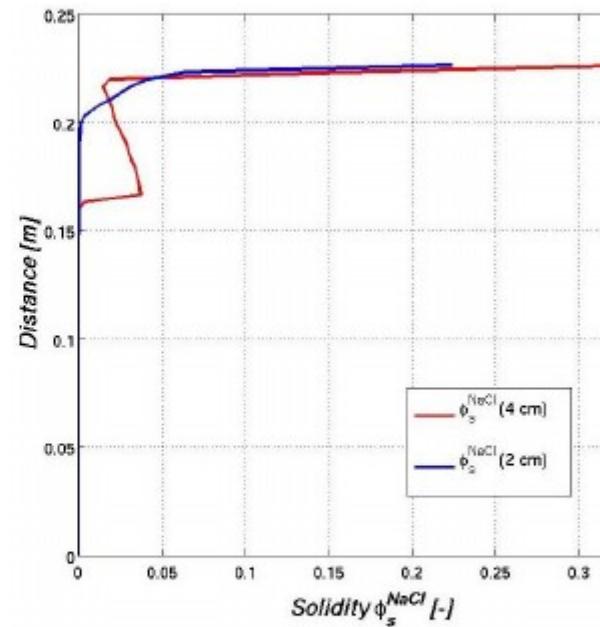
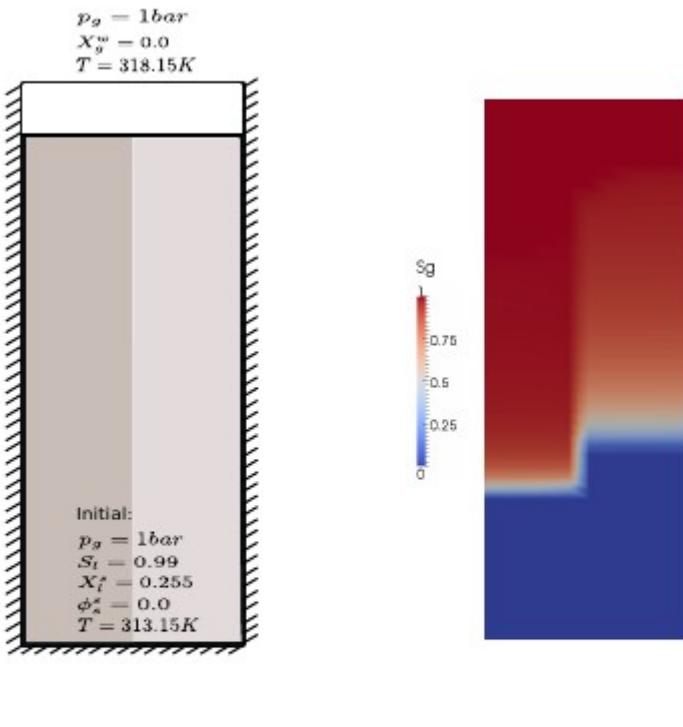
- No flow BC allows the domain to dry out with evaporation.
- Far-field dirichlet BC are used at top boundary.

Single-domain PM problem: Case III



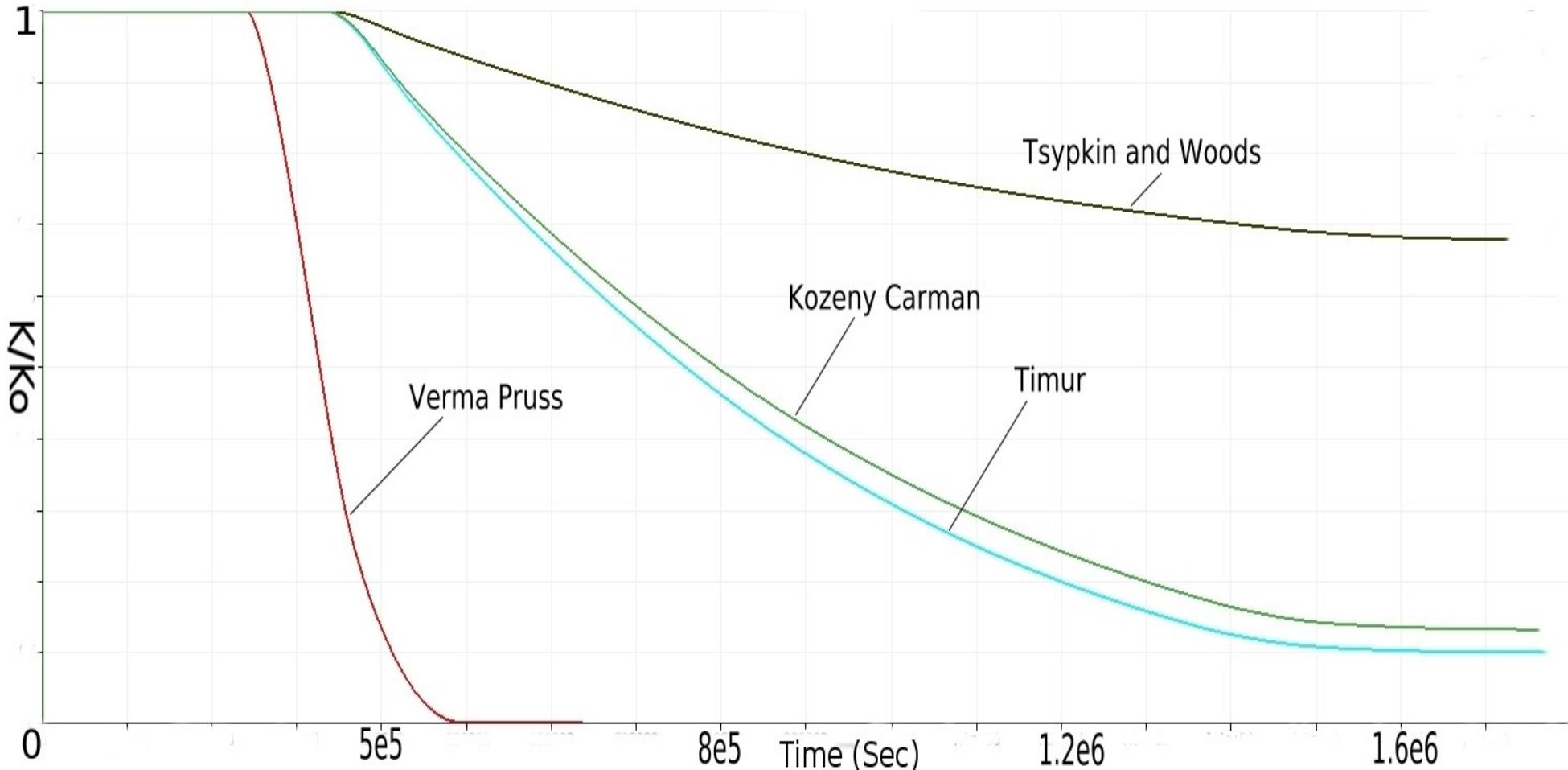
Movie: Evaporation driven NaCl precipitation in an unsaturated heterogeneous sand column

Single-domain PM problem: Case III



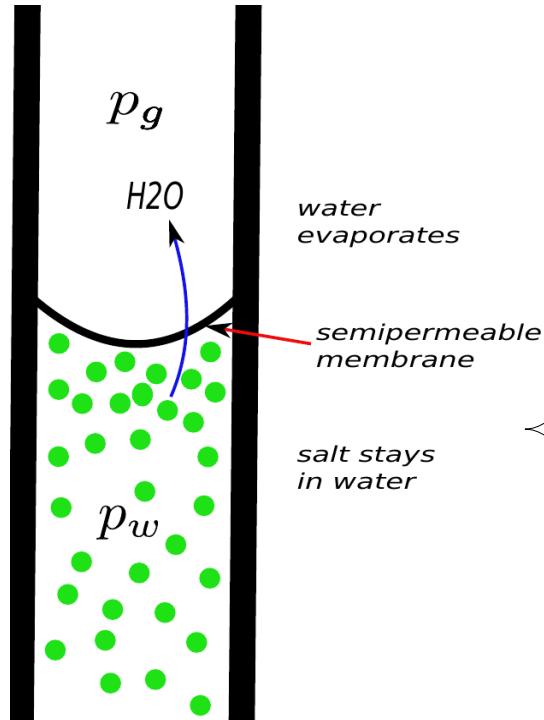
Evaporation driven NaCl precipitation in an unsaturated heterogeneous sand column

Single-domain PM problem: Case IV



- Different models need to be validated against the experimental data.
- For further calculations Kozeny-Carman relationship is used.

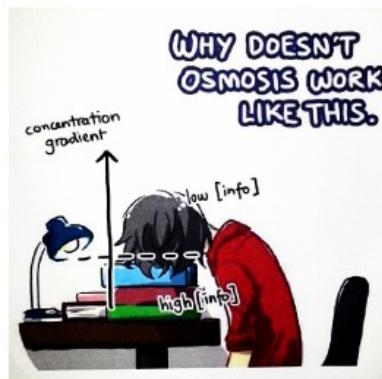
Osmotic potential & Vapour pressure



- Water-gas interface acts as a semi-permeable membrane
- Chemical equilibrium needed

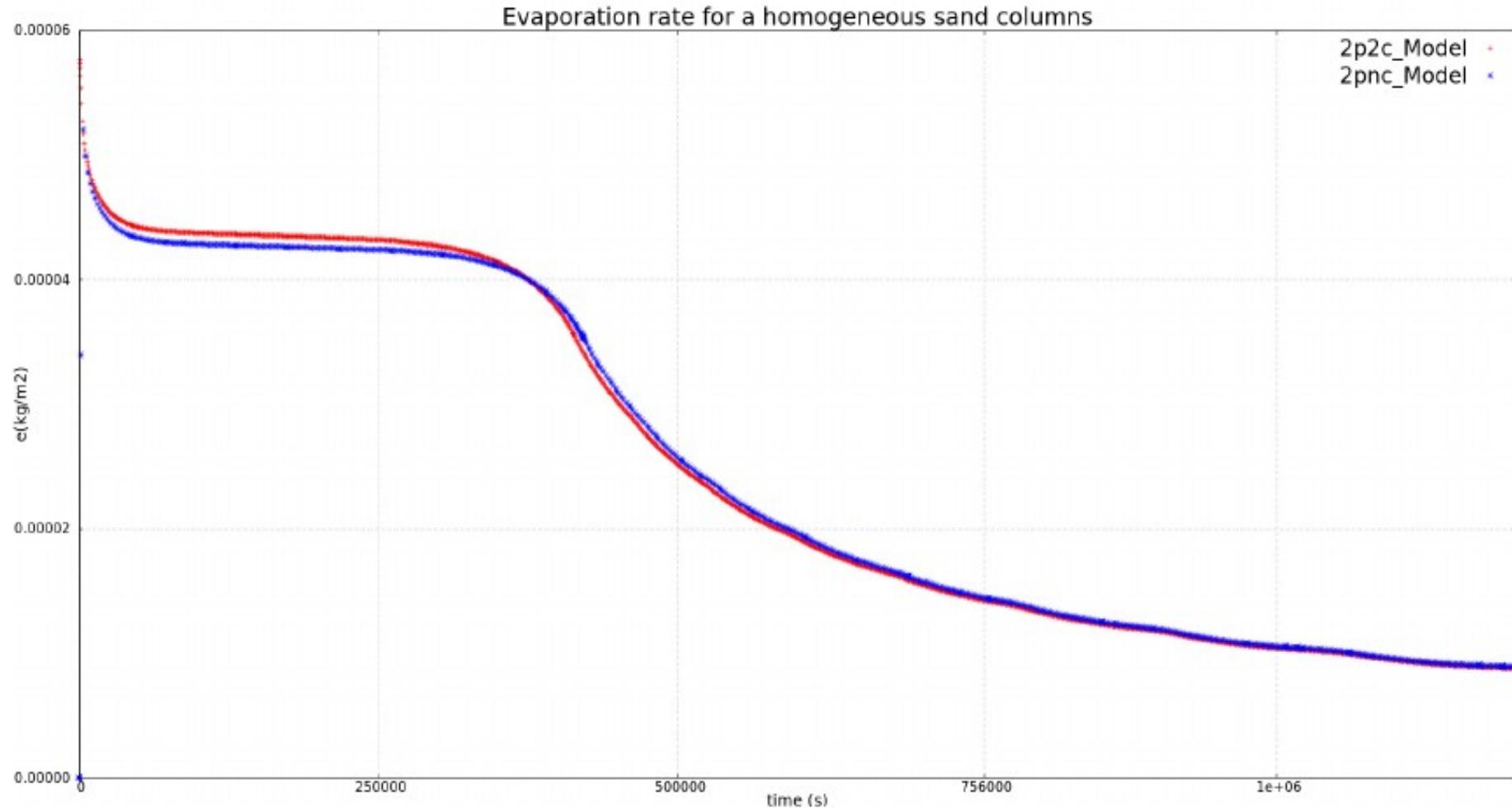
$$\psi_w(T, p_l, x_l^{NaCl}) = \psi_g(T, p_g, x_g^{NaCl} = 0)$$

$$f_l^{H2O} = f_g^{H2O} \implies p_{sat} x_l^{H2O} = p_g x_g^{H2O}$$



"Osmotically Driven Water Vapour transport in Unsaturated Soils", Kelly et.al., 2001

Evaporation: Pure water



- Comparison for pure water evaporation with the model presented by Mosthaf et.al (2011).