



# Developing numerical models for underground storage of synthetic natural gas

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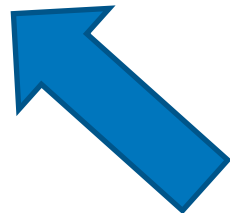
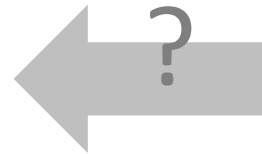
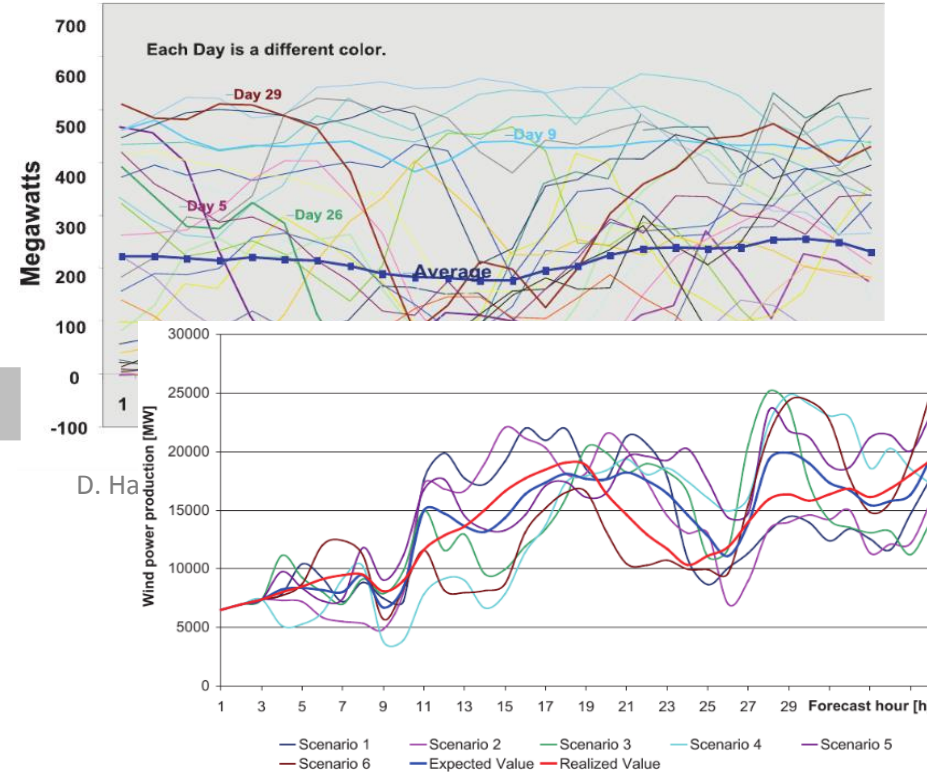
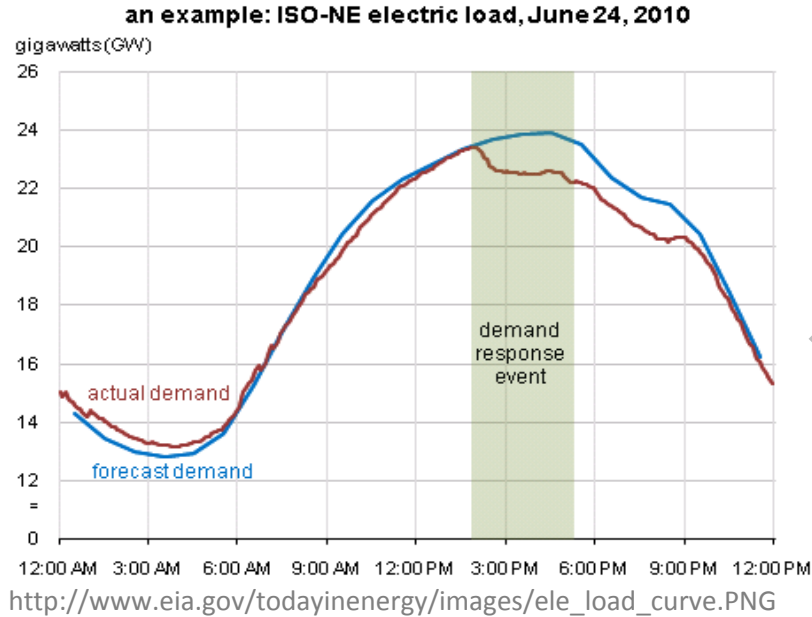
University of Stuttgart

In cooperation with Bo Guo and Mike Celia

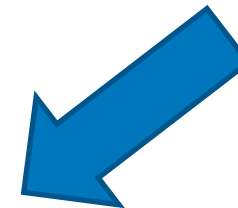
Princeton University



# Why energy storage?



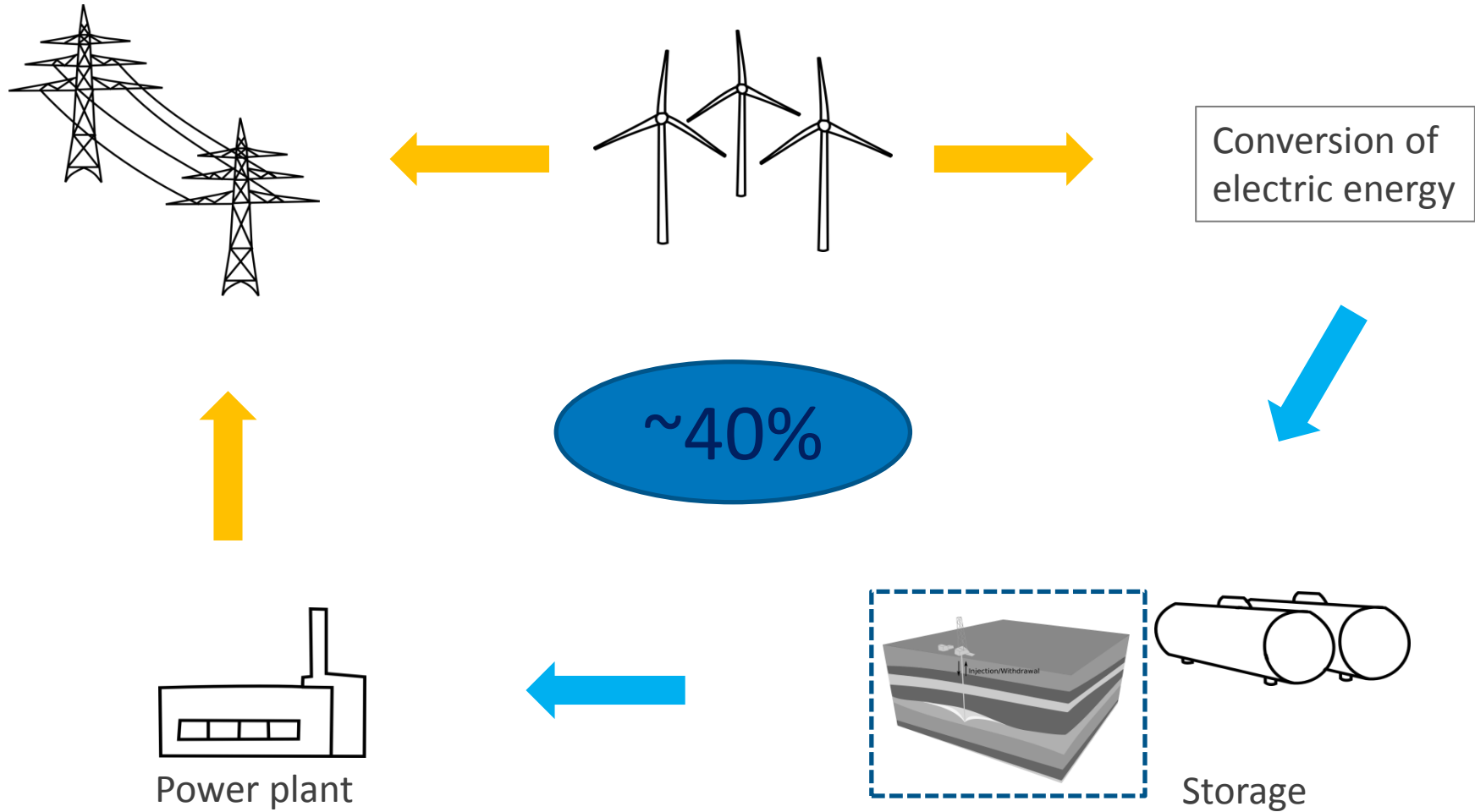
Energy storage



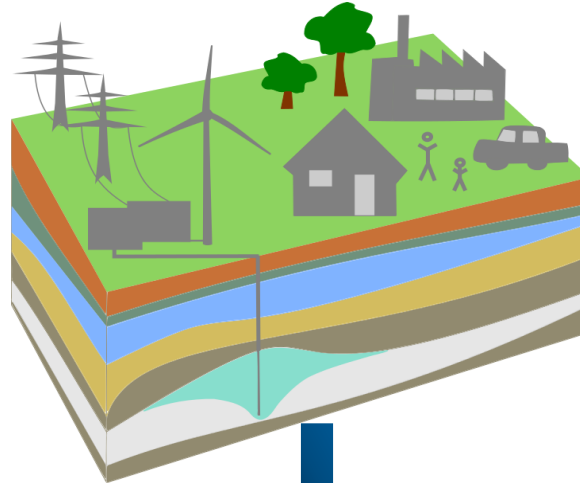
P. Meibom, et al.



# General renewable energy storage concept



## Subsurface energy storage options



Mechanical

Compressed air  
energy storage

Chemical

Hydrogen/SNG  
storage

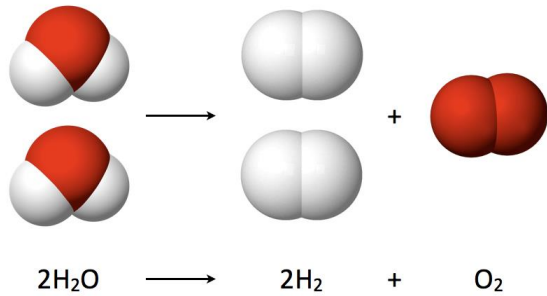
Thermal

Hot/cold water  
storage

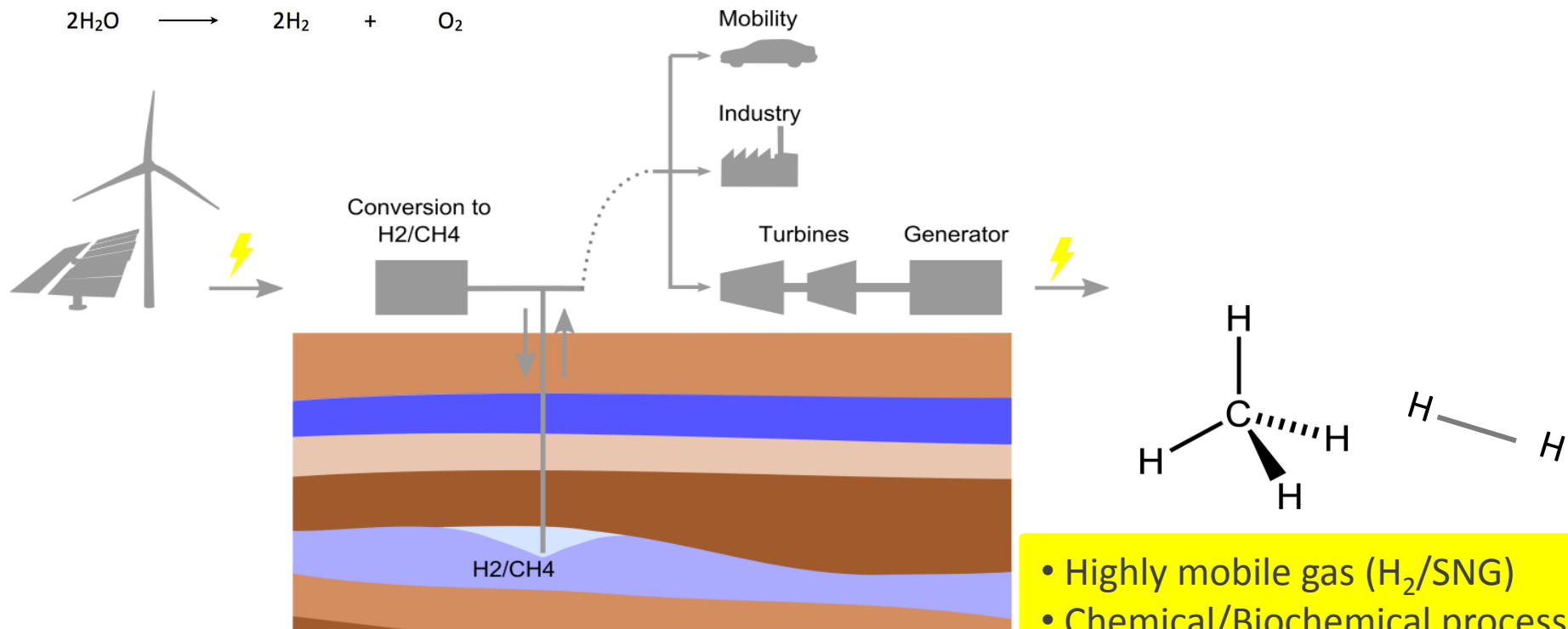
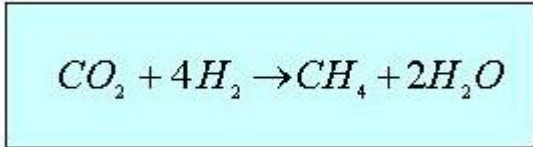


# Chemical underground energy storage

Electrolysis of water

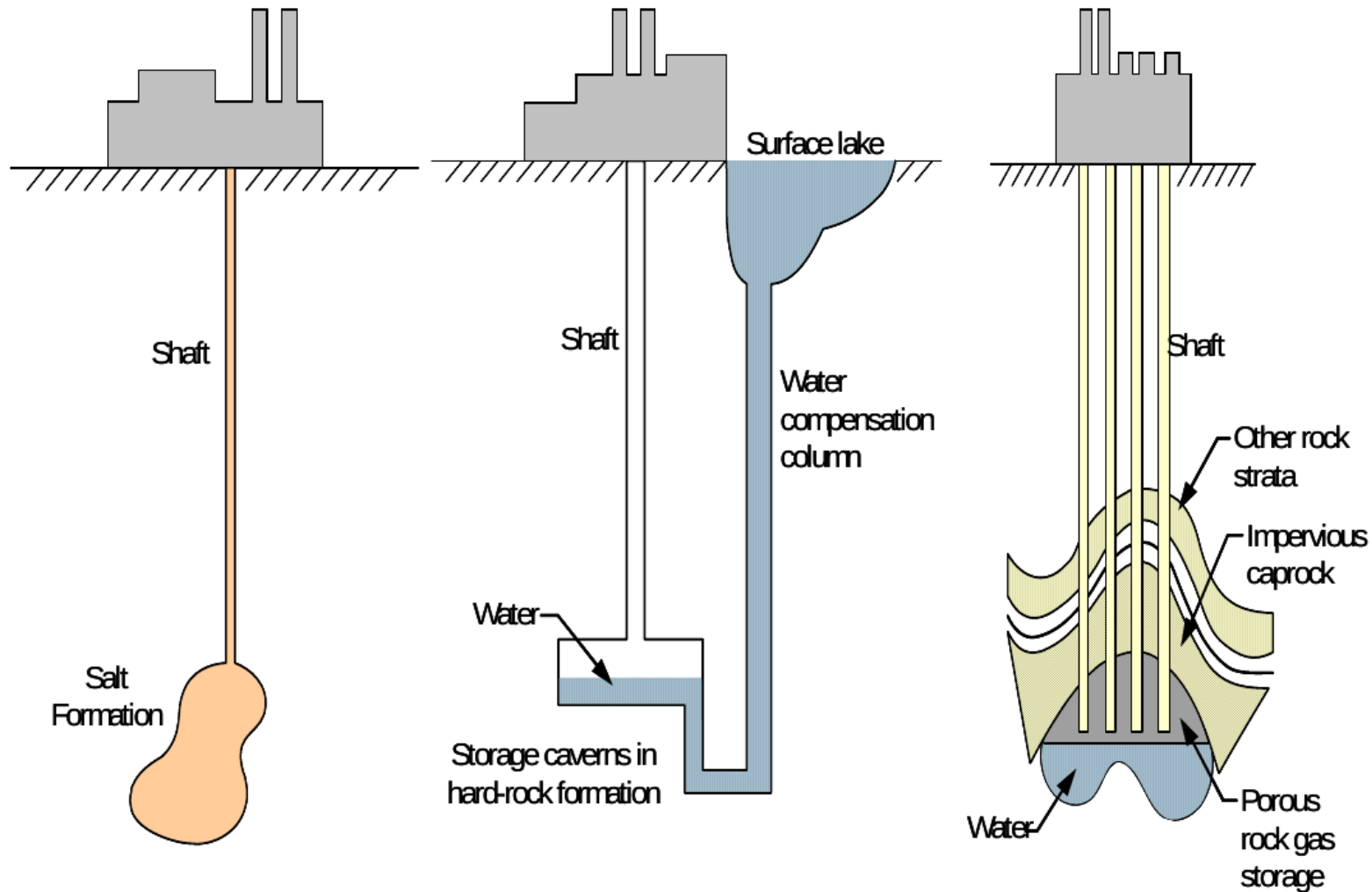


Sabatier reaction

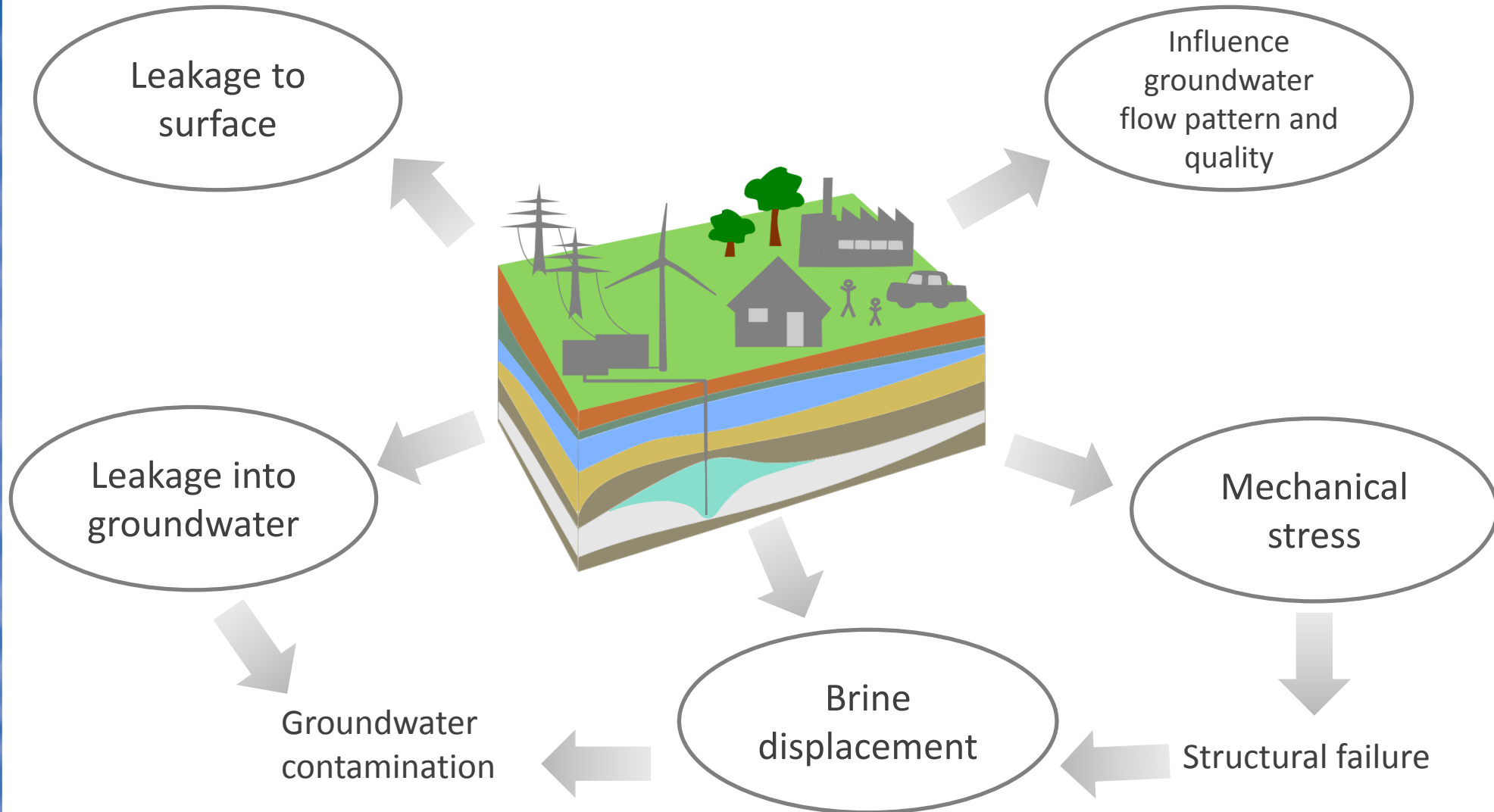


- Highly mobile gas (H<sub>2</sub>/SNG)
- Chemical/Biochemical processes

# Subsurface storage facilities



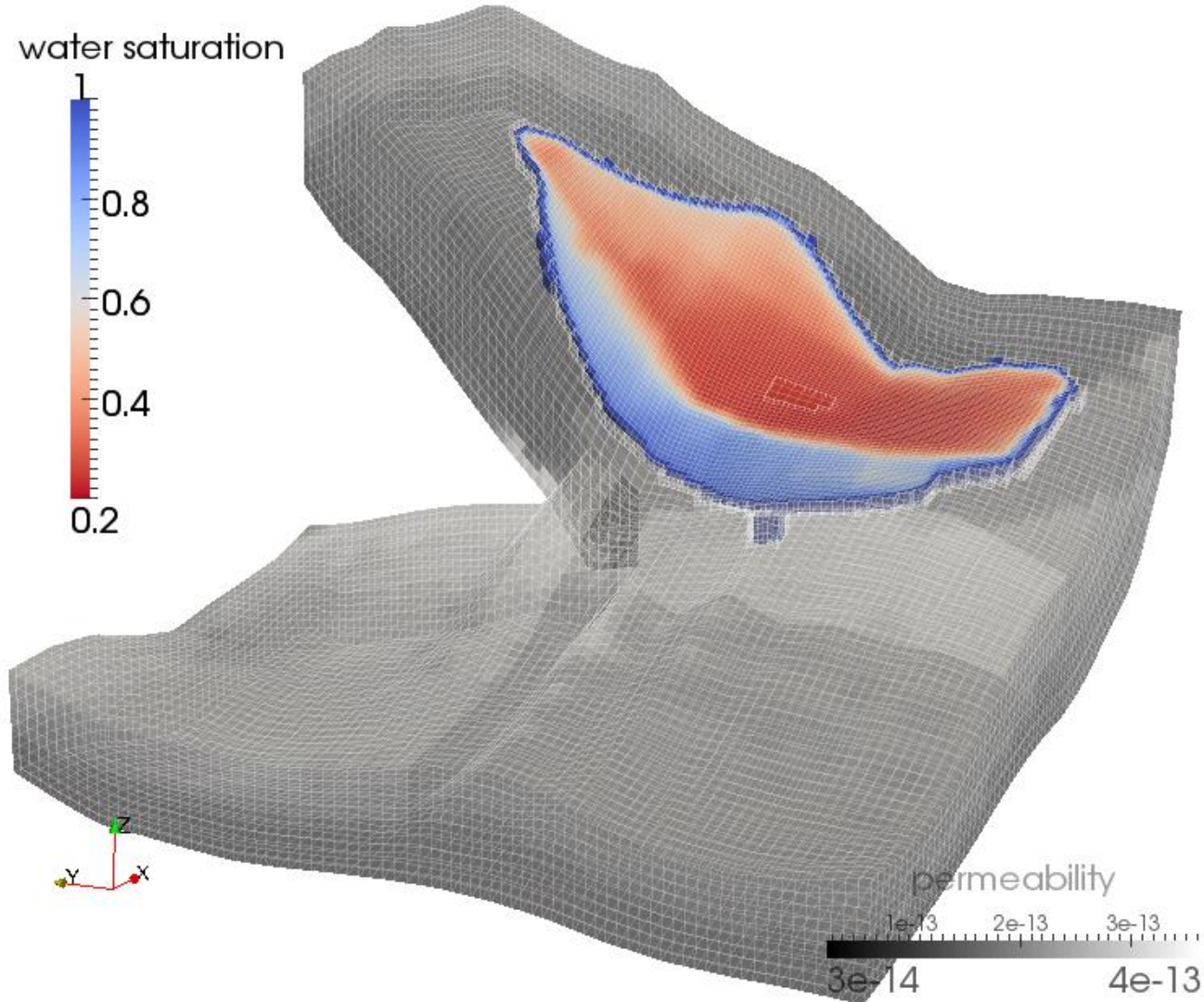
## Why modeling energy storage?







# Just a model...?

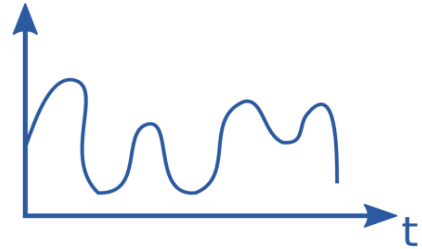






# Modeling challenges

injection rate



Injection

Withdrawal

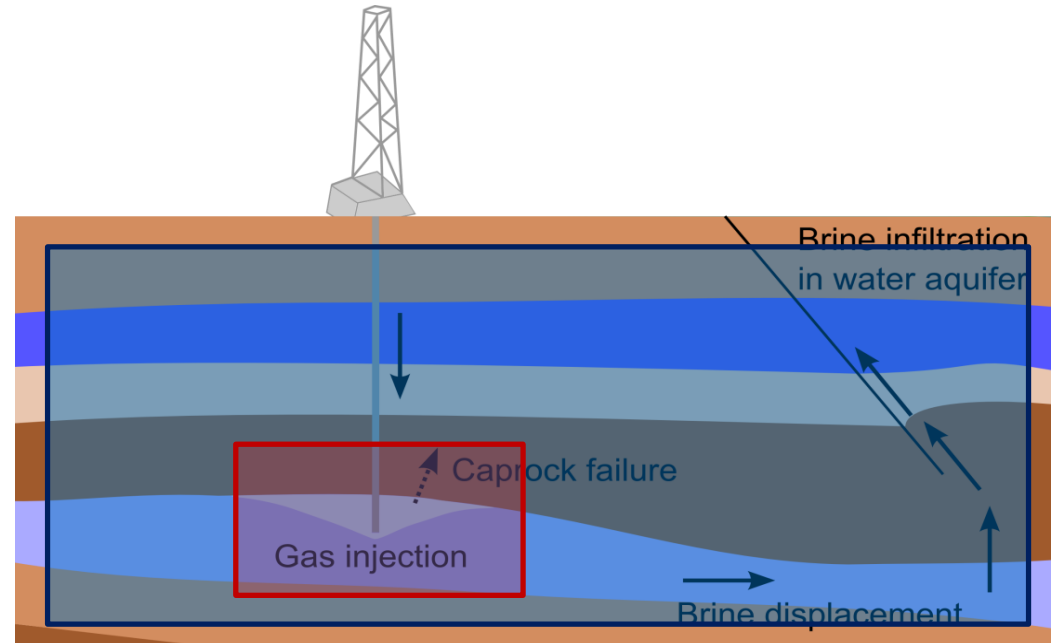
Fluctuations:  
- daily  
- weekly  
- seasonally

## Data:

- Limited data on geological parameters

## Processes:

- Multi phase flow
- Compositional effects
- Non-isothermal
- Fingering
- Strongly hysteretic



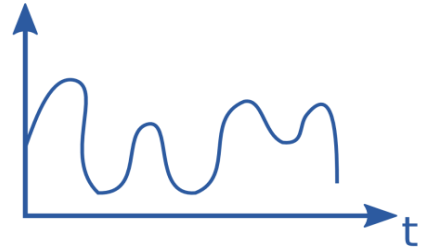
Highly complex

Less complex



# Modeling challenges

injection rate



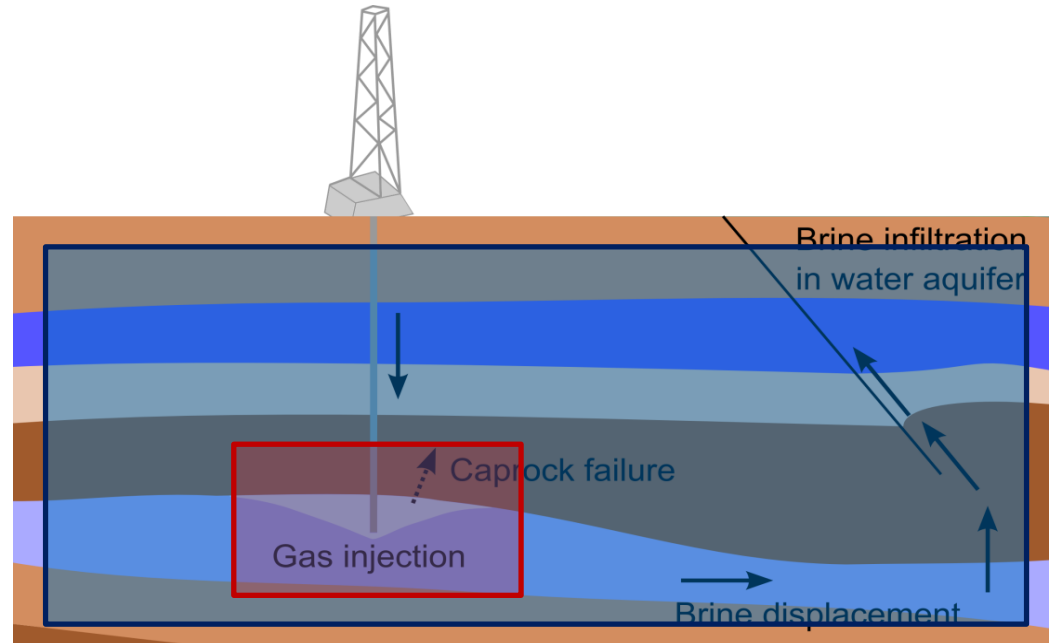
Injection

Withdrawal

Fluctuations:  
- daily  
- weekly  
- seasonally

## Time and spatial scales:

- Dynamic boundary conditions
- Large domains, relatively large time scales
- Local features (fault zones, brine displacement zone...)
- Locally highly complex processes, globally simple processes

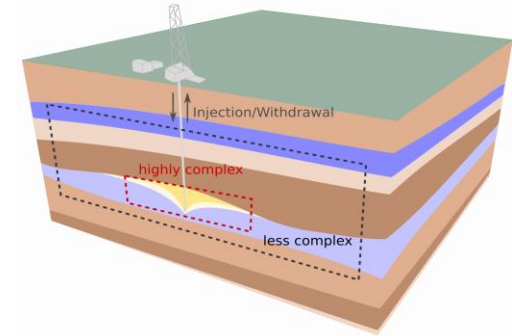


Highly complex

Less complex



# Adaptive modeling



Multi physics

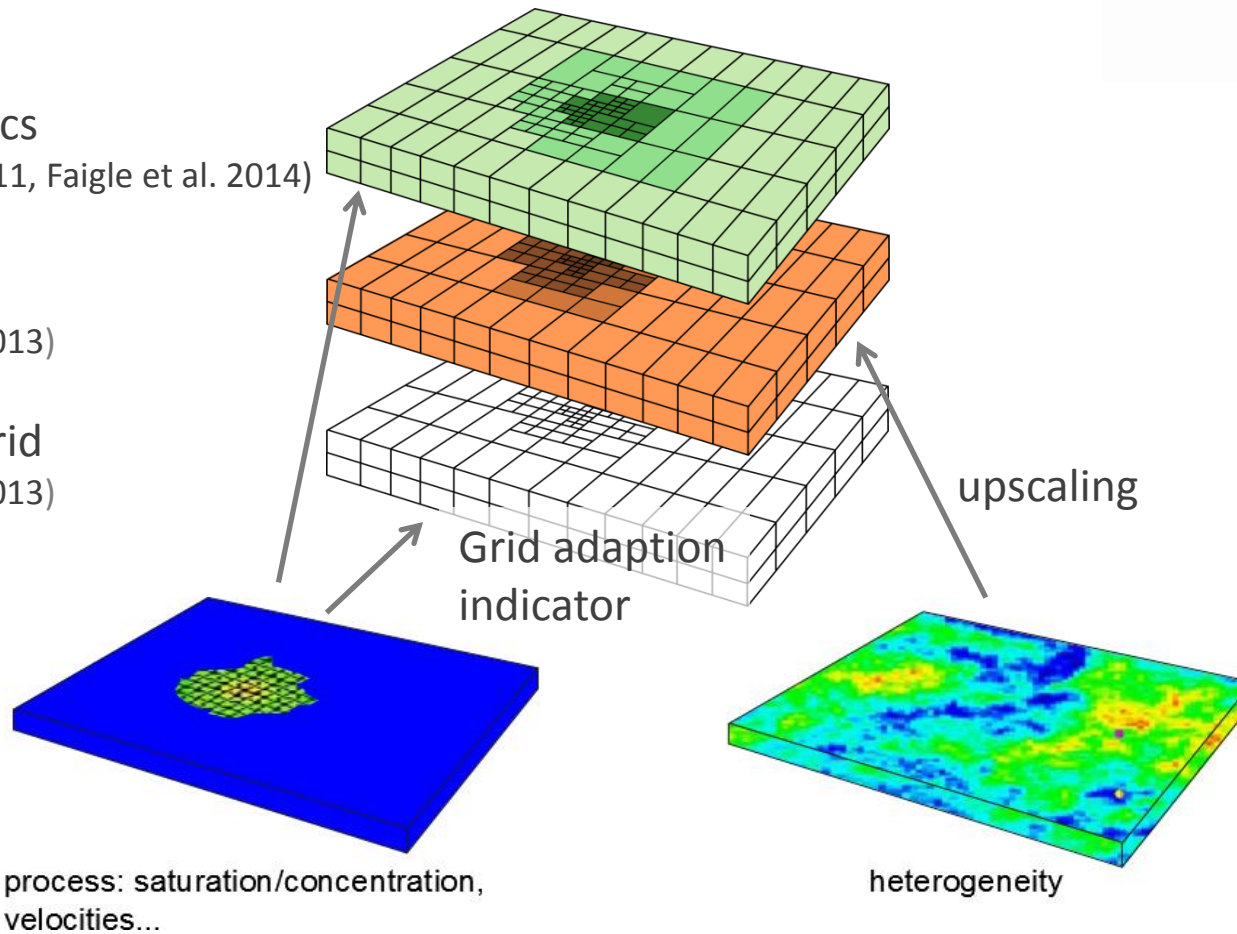
(Fritz et al. 2011, Faigle et al. 2014)

Multi scale

(Wolff et al. 2013)

Adaptive grid

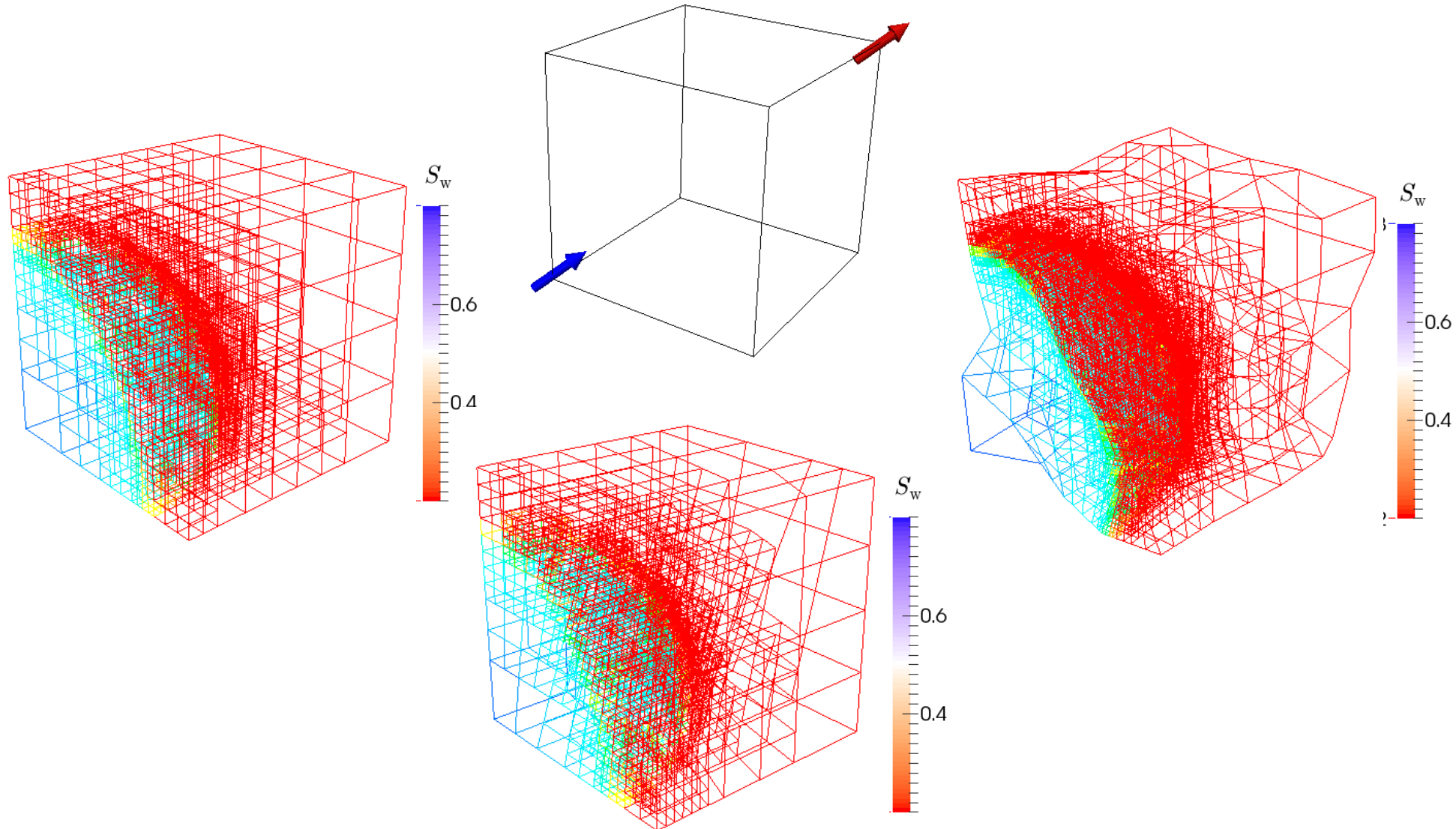
(Wolff et al. 2013)



process: saturation/concentration,  
velocities...

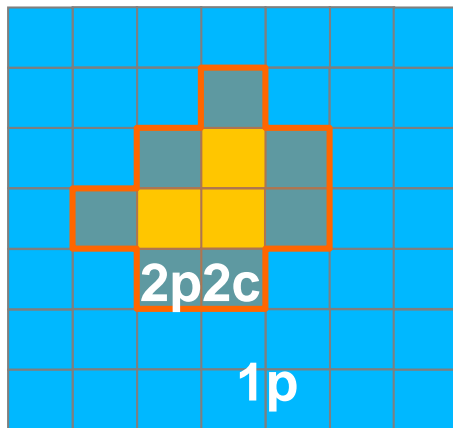
heterogeneity

# Adaptive grid example: Nine-spot water flow





## Multi-physics Modeling: Coupling (Fritz et al. 2011)



- Only one phase present in global rest domain.
- 2p2c processes only in subdomain.
- Only flux of one phase across subdomain border
- Dynamic subdomain: cell and all neighbors belong to subdomain if  $S \neq 1$

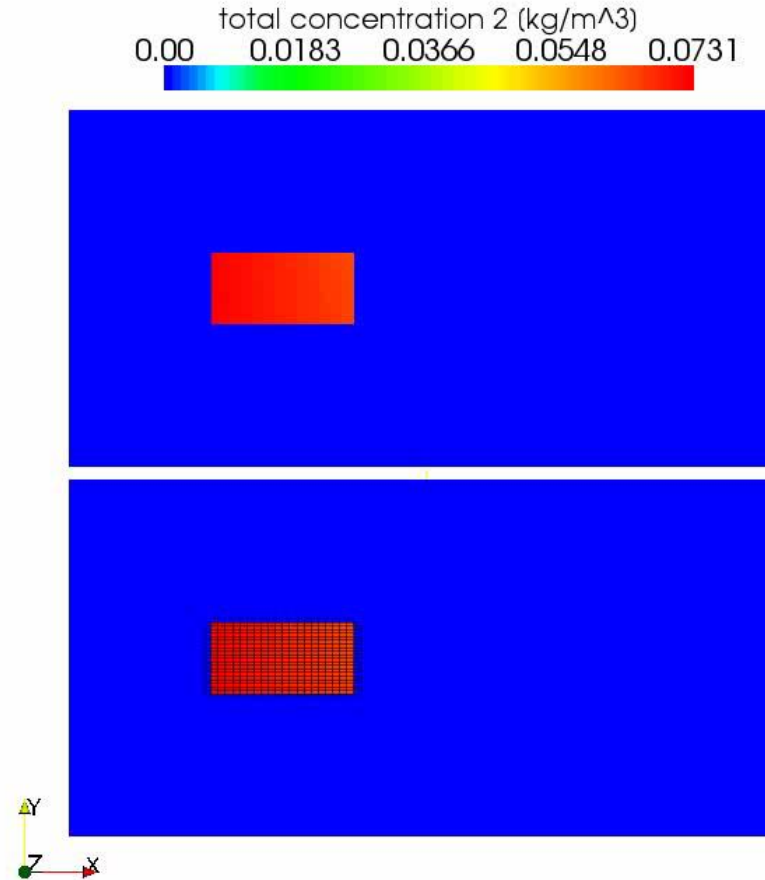
- Easy coupling of transport equations:

$$\frac{\partial C^{\kappa}}{\partial t} = - \sum_{\alpha} \nabla \cdot (\mathbf{v}_{\alpha} \rho_{\alpha} X_{\alpha}^{\kappa}) + q^{\kappa}$$

- 2p2c equation for a single phase equals: 
$$\frac{\partial C^{\kappa}}{\partial t} = \nabla \cdot \left( \frac{\mathbf{v}}{\phi} C^{\kappa} \right)$$



## Example: Two-phase two component





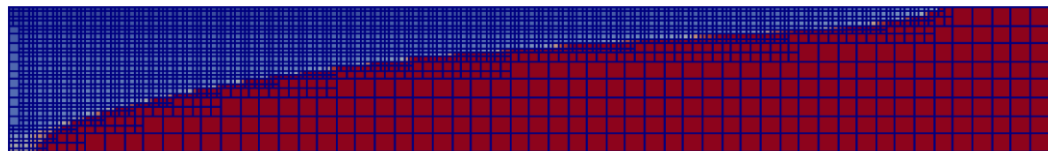


## Multi-Multi results:

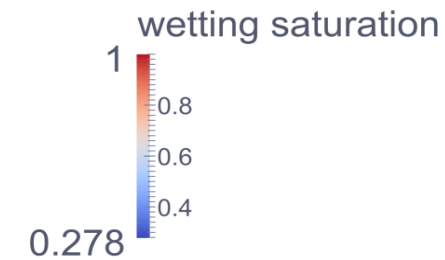
2D, injection of gas into a brine aquifer, 2phase-2component flow, isothermal



Adaptive grid:



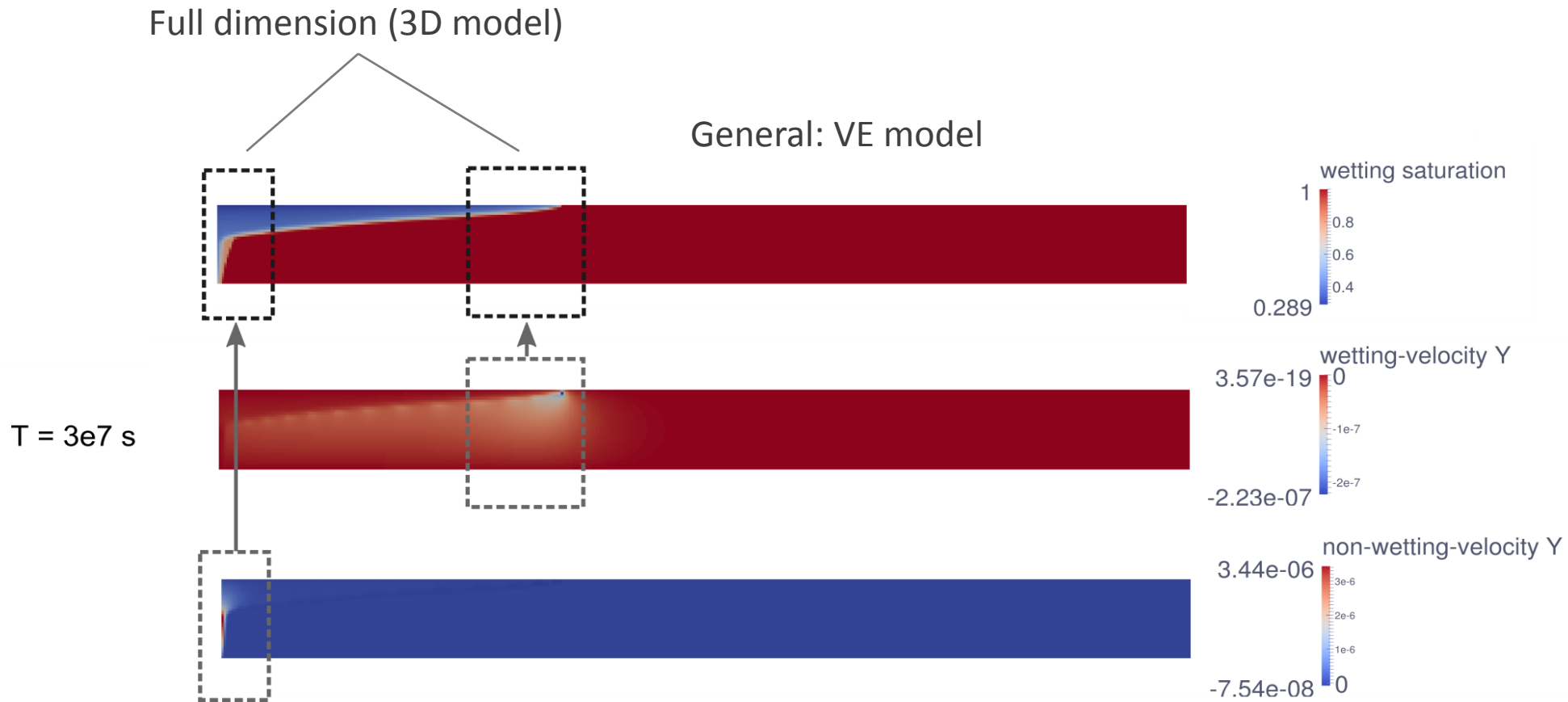
Multi-physics:



CPU time:  
Fully Implicit: 100%  
Impes: 14%  
Impes+Multi physics: 11%  
Impes+Adaptive: 2%



# Coupling of a VE to a 3D model





# Adaptive modeling

Multi dimensions

Multi physics

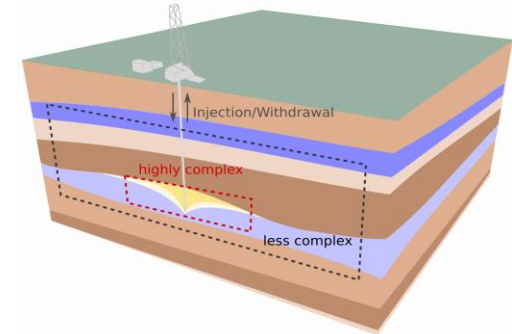
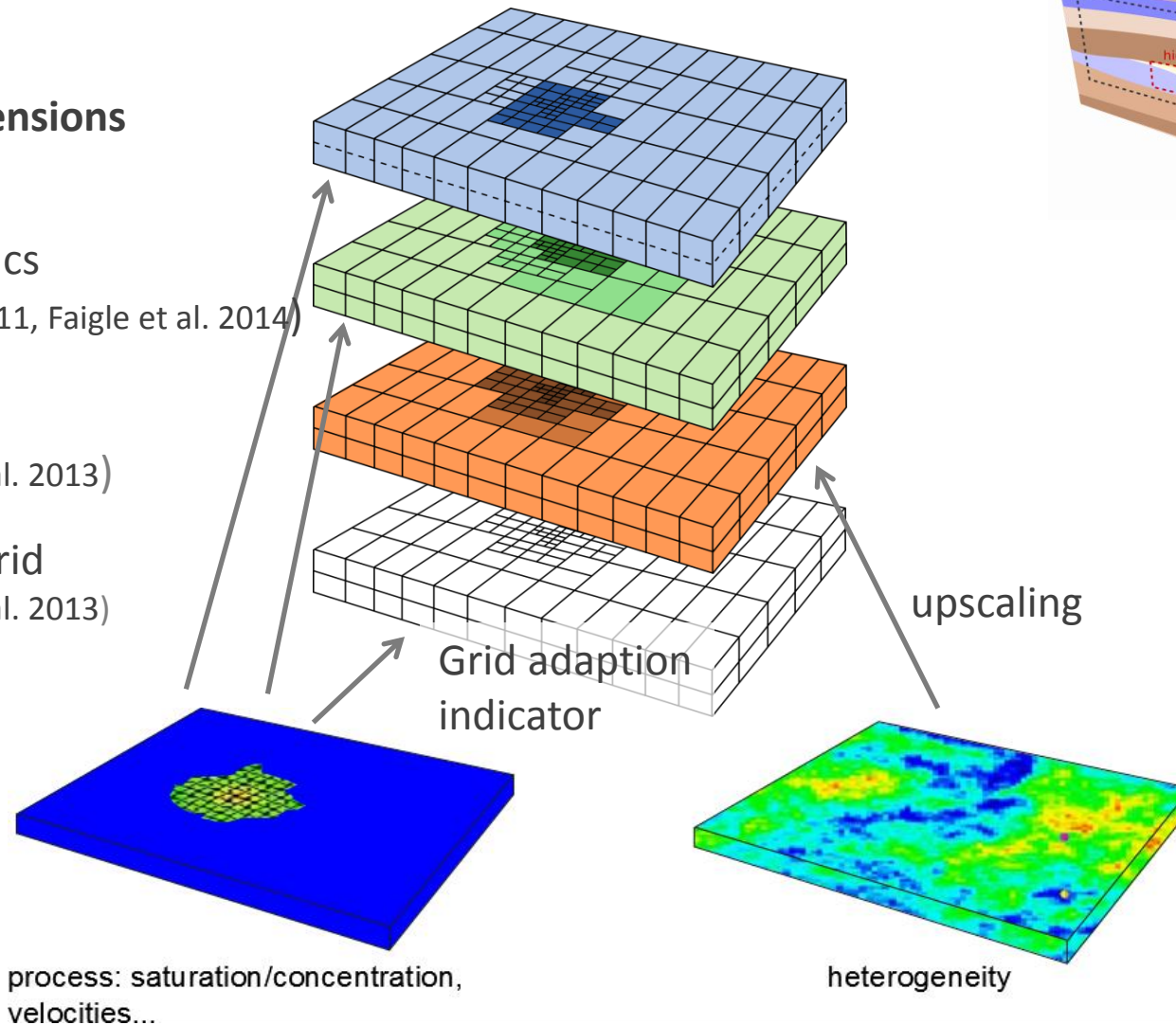
(Fritz et al. 2011, Faigle et al. 2014)

Multi scale

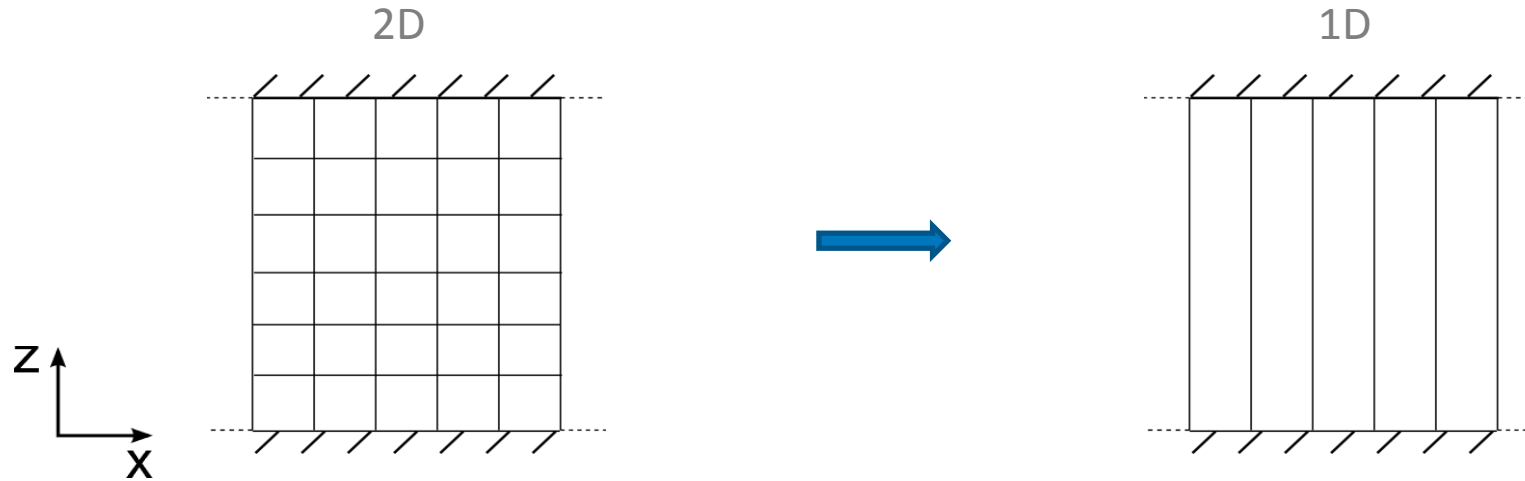
(M. Wolff, et al. 2013)

Adaptive grid

(M. Wolff, et al. 2013)



## VE model



$$\frac{\partial}{\partial t}(\rho_\alpha \phi s_\alpha) + \nabla \cdot (\rho_\alpha \mathbf{u}_\alpha) = \rho_\alpha \psi^\alpha \quad \frac{\partial}{\partial t}(\rho_\alpha \Phi S_\alpha) + \nabla \cdot (\rho_\alpha \mathbf{U}_\alpha) = \rho_\alpha \Psi^\alpha$$

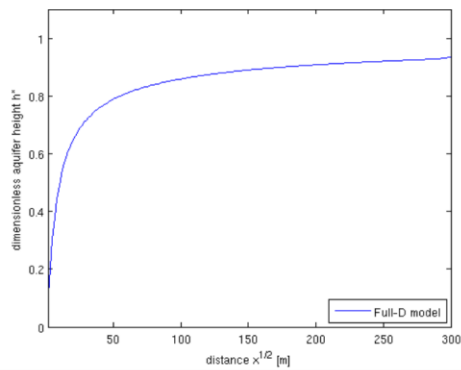
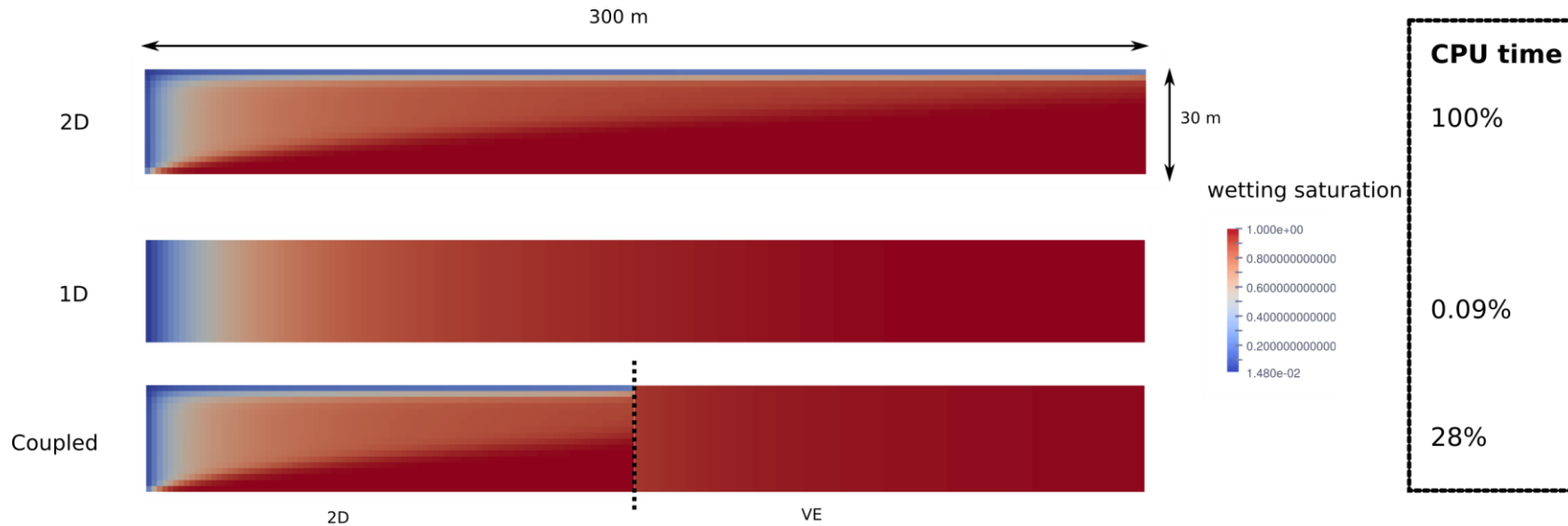
$$\mathbf{u}_\alpha = -\frac{k_{r,\alpha} \mathbf{k}}{\mu_\alpha} (\nabla p_\alpha - \rho_\alpha \mathbf{g})$$

$$\mathbf{U}_\alpha = -\mathbf{K} \Lambda_\alpha (\nabla P_\alpha - \rho_\alpha \mathbf{G})$$

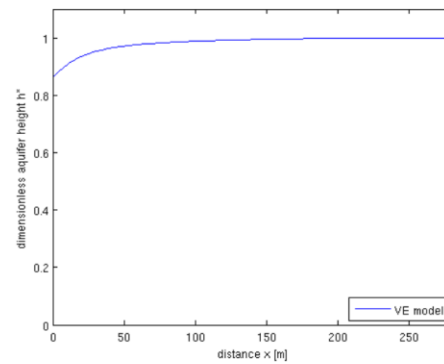
(B. Guo, et al. 2014)



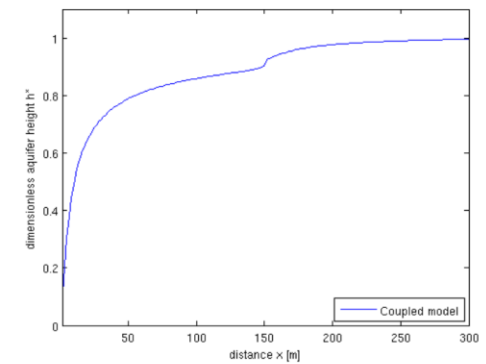
# Preliminary results



2D



1D



Coupled



## Summary and outlook

### First steps:

- Coupling of VE model to 3D model
- Model switching criteria → adaptive coupling
- In cooperation with Bo Guo and Mike Celia, Princeton University

Including heterogeneity

Including hysteresis (Papafotiou, et al. 2010)

Including multi-physics



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